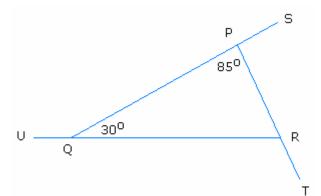
CHAPTER 7 Geometric Relationships 7.1 Angle Relationships in Triangles Interior and Exterior Angle Relationships for Triangles

The sum of the exterior angles of a triangle is 360°.

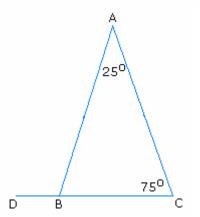
The exterior angle at each vertex of a triangle is equal to the sum of the interior angles at the other two vertices.

Example:

a) Find the measures of the exterior angles of Δ PQR.



b) Find the measure of \angle ABD.



Solution:

a)
$$\angle SPR + 85^{\circ} = 180^{\circ}$$

$$\angle SPR + 85^{\circ} - 85^{\circ} = 180^{\circ} - 85^{\circ}$$

$$\angle SPR = 95^{\circ}$$

$$\angle PQU + 30^{\circ} = 180^{\circ}$$

$$\angle PQU + 30^{\circ} - 30^{\circ} = 180^{\circ} - 30^{\circ}$$

$$\angle PQU = 150^{\circ}$$

$$\angle TRQ + \angle SPR + \angle PQU = 360^{\circ}$$

$$\angle TRQ + 95^{\circ} + 150^{\circ} = 360^{\circ}$$

$$\angle TRQ + 95^{\circ} - 150^{\circ} = 360^{\circ} - 95^{\circ} - 150^{\circ}$$

$$\angle TRQ = 115^{\circ}$$

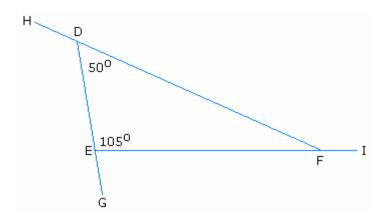
The measures of the exterior angles are \angle SPR = 95°, \angle PQU = 150°, and \angle TRQ = 115°.

b)
$$\angle ABD = \frac{25^{\circ} + 75^{\circ}}{100^{\circ}}$$

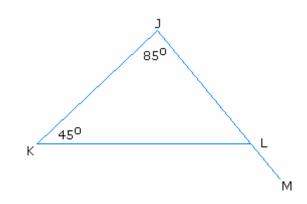
The measure of $\angle ABD = 100^{\circ}$.

Practice:

1. a) Find the measures of the exterior angles of $\Delta \text{DEF}.$



b) Find the measure of \angle KLM.



Answers:

- 1. a) \angle GEF = 75°, \angle HDE = 130°, and \angle IFD = 155°.
- b) $\angle KLM = 130^{\circ}$