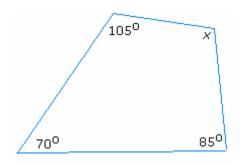
CHAPTER 7 Geometric Relationships 7.2 Angle Relationships in Quadrilaterals Interior and Exterior Angle Relationships in a Quadrilateral

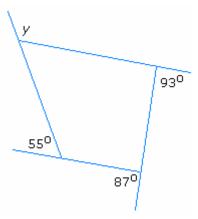
The sum of the interior angles in a quadrilateral is 360°. The sum of the exterior angles in a quadrilateral is 360°.

Example:

a) Find the measure of the unknown angle shown.



b) Find the measure of the unknown angle shown.



c) Find the unknown angles shown in the parallelogram.

Solution:

a)
$$x + 85^{\circ} + 70^{\circ} + 105^{\circ} = 360^{\circ}$$

 $x + 260^{\circ} = 360^{\circ}$
 $x + 260^{\circ} - 260^{\circ} = 360^{\circ} - 260^{\circ}$
 $x = 100^{\circ}$

The unknown angle $x = 100^{\circ}$.

b)
$$y + 93^{\circ} + 87^{\circ} + 55^{\circ} = 360^{\circ}$$

 $y + 235^{\circ} = 360^{\circ}$
 $y + 235^{\circ} - 235^{\circ} = 360^{\circ} - 235^{\circ}$
 $y = 125^{\circ}$

The unknown angle $y = 125^{\circ}$.



c) Adjacent angles are supplementary in a parallelogram.

$$x + 60^{\circ} = 180^{\circ}$$

 $x + 60^{\circ} - 60^{\circ} = 180^{\circ} - 60^{\circ}$
 $x = 120^{\circ}$

The unknown angle $x = 120^{\circ}$.

Angles at opposite vertices are equal.

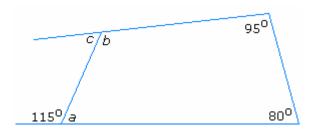
The unknown angle $y = 60^{\circ}$.

$$z = x$$
$$= 120^{\circ}$$

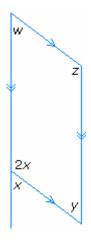
The unknown angle $z = 120^{\circ}$.

Practice:

1. a) Find the measure of the unknown angles shown.



b) Find the unknown angles shown.



Answers:

1. a)
$$a = 65^{\circ}$$
, $b = 120^{\circ}$, $c = 60^{\circ}$

b)
$$x = 60^{\circ}$$
, $2x = 120^{\circ}$, $w = 60^{\circ}$, $y = 60^{\circ}$, $z = 120^{\circ}$