Chapter 3 Practice Test

For questions 1 to 5, select the best answer.

- 1. The number of cells in a bacteria colony doubles every week. If N represents the number of cells in the colony, N_0 represents the number of cells at the start, and t represents the time, in days, then the expression that describes the situation is
 - **A** $N = N_0(2)^t$ **B** $N = 2(N_0)^t$ **C** $N_o = N(2)^t$
 - $\mathbf{D} \ N_o = \mathbf{2}(N)^t$
- 2. Compared to $y = 4^x$, the graph of $y = 4^{x-1}$ is translated
 - A 1 unit to the left
 - **B** 1 unit to the right
 - C 1 unit up
 - **D** 1 unit down

3. The range for the function $y = \frac{1}{2}(3)^x - 2$ is

$$A \{x \in \mathbb{R} \}$$
$$B \{x \in \mathbb{R}, x > -2\}$$
$$C \{y \in \mathbb{R}, y > 2\}$$
$$D \{y \in \mathbb{R}, y > -2\}$$

4. When simplified, the value of the expression

$$\left(\frac{1}{16}\right)^{-\frac{3}{4}} \text{ is}$$
A $\frac{1}{8}$
B $\frac{1}{16}$
C 8
D 16

- 5. The graph of $y = 4^x$ compared to the graph of $y = 2^{2x}$ would
 - A be a vertical stretch
 - **B** be a horizontal stretch
 - C be translated to the right
 - **D** be the same

6. Evaluate. Express your answers using only positive exponents.

a)
$$\left(\frac{1}{4}\right)^{-\frac{5}{2}}$$

b) $\left(\frac{1}{2}\right)^{0} + \left(\frac{1}{2}\right)^{-1} + \left(\frac{1}{2}\right)^{-2}$
c) $\left(-\left(-3\right)^{2}\right)^{-1}$
d) $\left(\frac{4}{9}\right)^{-\frac{3}{2}} + \left(\frac{1}{25}\right)^{-\frac{1}{2}}$

7. Simplify. Express your answers using only positive exponents.

a)
$$\left(x^{\frac{3}{2}}y^{-2}\right)^{-2}$$

b) $\left(2v^{-2}w^{2}\right)^{-3}\left(4v^{2}w^{2}\right)^{3}$
c) $\left(\frac{a^{2}b^{3}}{3}\right)^{-1} \times \left(\frac{4}{a^{-1}b^{3}}\right)^{2}$
d) $\sqrt[3]{27u^{3}v^{-6}}$

8. Describe the transformations of the function $y = 2^x$ that are needed to generate the

function
$$y = 2\left(\frac{1}{2}\right)^{x+1} + 2$$
.

- **9.** The population of a developing city increases by 8% per year. In 2005, 125000 people lived in the city.
 - a) Model the population as an exponential function, using t = 0 to represent the year 2005.
 - **b)** Graph the function for t = 0 to t = 20.
 - c) What is the population expected in 2020?
 - **d)** In what year should the population reach half a million?
 - e) What assumptions are made in order to answer parts c) and d)?



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10. To calculate interest, a financial institution uses

the formula $A = P\left(1 + \frac{i}{N}\right)^{n \times N}$, where A

represents the current amount, in dollars, of the investment; P is the principal invested; i is the annual interest rate, expressed as a decimal; N is the number of interest payments per year; and n represents the number of years of the investment.

- a) Rewrite the formula to express the principal amount, *P*, as a function of *A*, the amount invested.
- **b)** An account with a current balance of \$3590 has earned interest for 3 years at the rate of 6% per year, compounded monthly. What is the original amount of the principal invested?
- 11. The formula for the surface area, *S*, of a cylinder is $S = 2\pi r^2 + 2\pi rh$, where *h* is the height of the cylinder and *r* is the radius.
 - a) Rewrite this formula to express the height as a function of the surface area and radius of the cylinder.
 - **b)** Rewrite the expression from part a) in another way.
 - c) If the surface area of the cylinder is 503 cm² and the diameter is 10 cm, what is the height of the cylinder?

12. The table shows data collected by scientists studying the polar bear population in a remote area of the Arctic.

Year	Population
2000	825
2001	883
2002	945
2003	1011
2004	1081
2005	1157
2006	1238
2007	1325

- a) Modify this table of values such that t = 0 represents the year 2000.
- **b)** Make a scatter plot of the data.
- c) Do the data appear to be exponential in nature? Explain.
- d) Find the equation of the curve of best fit.
- e) Use this equation to determine the polar bear population expected in 2012.
- **f)** How long will it take the population to reach 4500, assuming the pattern of growth continues?

