6.5 Geometric Sequences

1. Determine the common ratio for each geometric sequence.

a) 3, 12, 48, 192, ...
b)
$$\frac{1}{3}$$
, -1, 3, -9, ...
c) $\frac{1}{4}$, $\frac{1}{8}$, $\frac{1}{16}$, $\frac{1}{32}$, ...
d) 1000, -500, 250, -125, ...

2. Write the first five terms of each geometric sequence.

a)
$$t_1 = 2, t_2 = -6$$

b) $t_1 = 40, t_2 = 20$
c) $t_n = \frac{1}{8} (4)^{n-1}$
d) $t_n = -2 (-5)^{n-1}$

3. Determine the number of terms in each geometric sequence.

a) 3, 21, 147, 1029, ..., 2 470 629
b)
$$\frac{1}{3}$$
, $\frac{2}{3}$, $\frac{4}{3}$, $\frac{8}{3}$, ..., $\frac{512}{3}$
c) 3, -9, 27, -81, ..., 177, 147
d) $\frac{2}{25}$, $\frac{2}{5}$, 2, 10, ..., 6250

4. Determine whether each sequence is arithmetic, geometric, or neither. If it is arithmetic, state the values of *a* and *d*. If it is geometric, state the values of *a* and *r*.

a) 500, 125, ¹²⁵/₄, ¹²⁵/₁₆, ...
b) 11, 14, 18, 23, 29, ...
c) 7, 14, 28, 56, ...
d) 11, 14, 17, 20, 23, ...

5. Find the term number in the geometric sequence 3, 6, 12, 24, ... that has a value of 1536.

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- 6. To try to break a world record, a set of dominoes is set up such that every 10th domino that falls causes 3 dominoes to fall. As a result, after the one line that starts the fall, the 10th domino causes 3 lines to start to fall. Once each of these has progressed to their 10th domino, each of these causes 3 new lines to start to fall. How many lines will start to fall if this pattern is repeated 4 times?
- **7.** A strain of bacteria doubles every 14 h. If there are 100 bacteria cells to start with in a colony, how many will there be after 7 days?
- **8.** The half-life of a radioactive material is 11 years. Initially, there were 16 000 mg of the material.
 - a) What are the values of *a* and *r* in this sequence?
 - **b)** Write the general term of the geometric sequence.
 - c) Use this general term to determine how much material would remain after
 - i) 55 years
 - **ii)** 121 years
 - iii) 99 years

