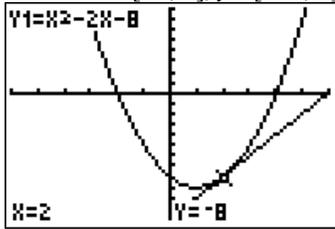


1.6 Slopes of Tangents and Instantaneous Rate of Change

BLM 1-17

1. Consider the graph shown.

Window: $x \in [-6, 6]$, $y \in [-12, 8]$ 

- a) Write the coordinates of the tangent point shown.
- b) Estimate and state the coordinates of another point on the tangent line.
- c) Determine the slope of the tangent using the points from parts a) and b).
- d) Draw the tangent to the curve at the point $(-1, -5)$. Estimate another point that is on this tangent line. Find the slope of this second tangent line.
- e) Interpret the significance of the differences in the values found in parts c) and d).
- f) Discuss what you predict the values will be of the slopes of tangents drawn at other points on the curve.
2. A projectile is shot into the air such that its height, h , in metres, after t seconds can be modelled by the function $h(t) = 25t - 4.9t^2$.
- a) Complete the table.
- | Interval | Δh | Δt | $\frac{\Delta h}{\Delta t}$ |
|-----------------------|------------|------------|-----------------------------|
| $4 \leq t \leq 4.1$ | | | |
| $4 \leq t \leq 4.01$ | | | |
| $4 \leq t \leq 4.001$ | | | |
- b) Use the table to estimate the velocity of the projectile after 4 s.
3. After t hours, the number of bacteria, N , in a culture can be modelled using the function $N(t) = 75\,000 + 64t^3$.
- a) Determine the average rate of change of the growth of the number of bacteria with respect to time for the first 6 h.
- b) Estimate the instantaneous rate of change of the number of bacteria after 6 h.
4. The displacement, s , in metres, of a particle moving back and forth in a straight line can be modelled by the function $s(t) = 4t^2 - 10t + 13$ where t is measured in seconds.
- a) Find the average rate of change of the distance with respect to time from 1 s to 4 s.
- b) Estimate the instantaneous rate of change of the displacement of the particle after 1 s.
- c) Sketch the curve and the tangent at $t = 1$.
- d) Interpret the average rate of change and the instantaneous rate of change for this situation.
5. The population, P , of a small town is modelled by the function $P(t) = -2t^3 + 55t^2 + 15t + 22\,000$, where $t = 0$ represents the beginning of this year.
- a) Write an expression for the average rate of change of population from $t = 10$ to $t = 10 + h$.
- b) Use the expression in part a) to determine the average rate of change of the population when
- i) $h = 3$ ii) $h = 5$
- c) Use the expression in part a) to estimate the instantaneous rate of change of the population after 10 years.
- d) Use **Technology** Graph $P(x)$.
- e) Using the graph from part d), would it be justified for a large department store to open 10 years from now in this town? Explain.
- f) If the store was not opened 10 years from now, would it be justified instead to open it 30 years from now? Explain.