

## Section 1.2 Summary

BLM 1-7

(page 1)

## Finite Differences

For a polynomial function of degree  $n$ , where  $n$  is a positive integer, the  $n$ th differences

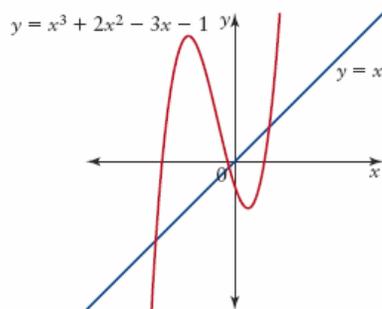
- are equal (or constant)
- have the same sign as the leading coefficient
- are equal to  $a[n \times (n - 1) \times \dots \times 2 \times 1]$ , where  $a$  is the leading coefficient

### KEY CONCEPTS

#### Key Features of Graphs of Polynomial Functions With Odd Degree

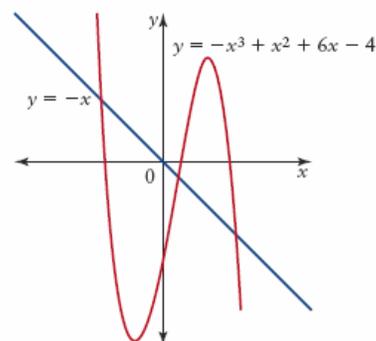
##### Positive Leading Coefficient

- the graph extends from quadrant 3 to quadrant 1 (similar to the graph of  $y = x$ )



##### Negative Leading Coefficient

- the graph extends from quadrant 2 to quadrant 4 (similar to the graph of  $y = -x$ )

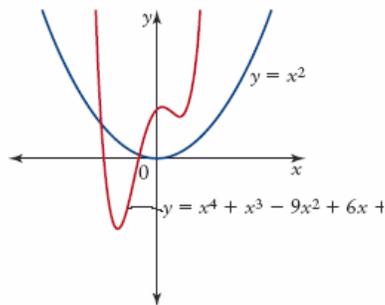


- Odd-degree polynomials have at least one  $x$ -intercept, up to a maximum of  $n$   $x$ -intercepts, where  $n$  is the degree of the function.
- The domain of all odd-degree polynomials is  $\{x \in \mathbb{R}\}$  and the range is  $\{y \in \mathbb{R}\}$ . Odd-degree functions have no maximum point and no minimum point.
- Odd-degree polynomials may have point symmetry.

## Key Features of Graphs of Polynomial Functions With Even Degree

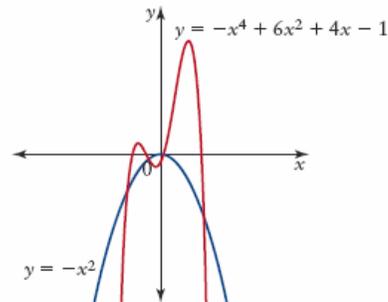
## Positive Leading Coefficient

- the graph extends from quadrant 2 to quadrant 1 (similar to the graph of  $y = x^2$ )
- the range is  $\{y \in \mathbb{R}, y \geq a\}$ , where  $a$  is the minimum value of the function
- an even-degree polynomial with a positive leading coefficient will have at least one minimum point



## Negative Leading Coefficient

- the graph extends from quadrant 3 to quadrant 4 (similar to the graph of  $y = -x^2$ )
- the range is  $\{y \in \mathbb{R}, y \leq a\}$ , where  $a$  is the maximum value of the function
- an even-degree polynomial with a negative leading coefficient will have at least one maximum point



- Even-degree polynomials may have from zero to a maximum of  $n$   $x$ -intercepts, where  $n$  is the degree of the function.
- The domain of all even-degree polynomials is  $\{x \in \mathbb{R}\}$ .
- Even-degree polynomials may have line symmetry.

## Key Features of Graphs of Polynomial Functions

- A polynomial function of degree  $n$ , where  $n$  is a whole number greater than 1, may have at most  $n - 1$  local minimum and local maximum points.
- For any polynomial function of degree  $n$ , the  $n$ th differences
  - are equal (or constant)
  - have the same sign as the leading coefficient
  - are equal to  $a[n \times (n - 1) \times \dots \times 2 \times 1]$ , where  $a$  is the leading coefficient