

1.5 Slopes of Secants and Average Rate of Change

BLM 1-15

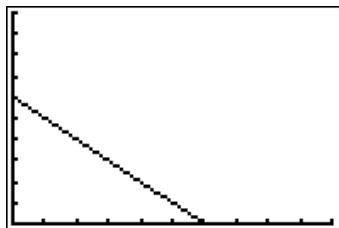
1. Identify whether the average rate of change for pairs of points along each graph is constant and positive, constant and negative, zero or non-constant.

Justify your response.

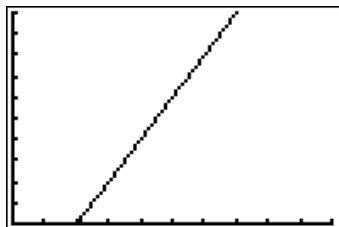
Window variables for all three graphs:

$x \in [0, 10]$, $y \in [0, 10]$.

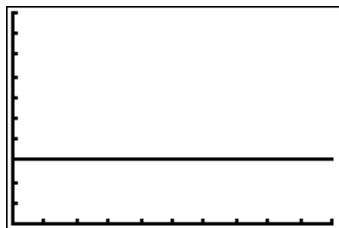
a)



b)



c)



2. Determine the average rate of change for two points on each line segment in question 1.

3. The cost, C , of making one unit of a product at any time x , in years, can be modelled by the function

$$C(x) = 4500 + 1530x - 0.04x^3,$$

$$x \in [0, 200].$$

- a) Determine algebraically the average rate of change of the cost from

i) year 0 to year 4

ii) year 4 to year 7

iii) year 7 to year 9

- b) Interpret your answers from part a).

4. If a ball is dropped from the top of a 120-m cliff, its height, h , in metres, after t seconds can be modelled by

$$h(t) = 120 - 4.9t^2.$$

- a) Find the average rate of change of the height of the ball with respect to time over the intervals

i) 1 s to 4 s

ii) 4 s to 6 s

iii) 6 s to 7 s

- b) What does the average rate of change represent in this situation?

- c) Interpret the significance of your answers in part a).

5. A census is taken of the permanent population, P , of Collingwood, Ontario every five years.

Year	Population
1991	13 500
1996	15 596
2001	16 039
2006	17 290

- a) Determine the average rate of change of the population for

i) 1991 to 1996

ii) 1996 to 2001

iii) 2001 to 2006

iv) the entire fifteen-year period

- b) What factors do you think might have led to the varied results?