

7.4 Techniques for Solving Logarithmic Equations

BLM 7-6

1. Solve algebraically.
 - a) $\log(x+5) = 2$
 - b) $1 - 2\log(p-8) = 0$
 - c) $\log_2(m+12) = 4$
2. **Use Technology** Solve using graphing technology.
 - a) $\log(x-2) = 1$
 - b) $2 - \log(v+1) = 0$
3. Solve. Identify and reject any extraneous roots.
 - a) $\log_2(x-5) + \log_2(x-2) = 2$
 - b) $\log x + 3 = \log(10x^3)$
 - c) $2\log m + 3\log m = 10$
4. Solve. Check for extraneous roots.
 - a) $\log(x+5)^3 = 3$
 - b) $\log \sqrt{x^2 - 5x + 9} = 1$
5. Solve.
 - a) $\log_2 x + \log_2(x-3) = 2$
 - b) $\log(x+2) = 2 - \log(x-3)$
6. **Use Technology** Find the roots of each equation, correct to two decimal places, using graphing technology. Sketch the graphical solution.
 - a) $\log x = 1 + \log(x-2)$
 - b) $4\log(x+1) - 5 = \log(x) - 2$
7. The number of years, n , required for an investment P_1 to grow to amount P_2 when interest is $i\%$ per year (expressed as a decimal) is given by the formula

$$n = \frac{\log P_2 - \log P_1}{\log(1+i)}.$$
 - a) How many years does it take for \$1500 to grow to \$2380 at a yearly interest rate of 8%?
 - b) How much should be invested, to the nearest dollar, in order for it to grow to be \$4137 in 8 years at a yearly rate of 5%?
 - c) What yearly interest rate is needed to allow \$900 to grow to \$1689 in 10 years, to the nearest tenth of a percent?
8. Solve $\log_2 \sqrt{x} + \log_4 x = 5$.
9. a) Calculate $(\log_2 5)(\log_5 8)(\log_8 10)$.
 b) Compare your answer from part a) to $\log_2 10$.
 c) Prove that $(\log_a b)(\log_b c)(\log_c d) = \log_a d$.