

# Rational Functions



## General Outcome

Develop algebraic and graphical reasoning through the study of relations.

## Specific Outcomes


**RF14** Graph and analyze rational functions (limited to numerators and denominators that are monomials, binomials or trinomials).

By the end of this chapter, students will be able to:

| Section | Understanding Concepts, Skills, and Processes  |
|---------|--|
| 9.1     | ✓ graph, analyse, and compare rational functions using transformations and using technology                                |
|         | ✓ examine the behaviour of the graphs of rational functions near non-permissible values.                                   |
| 9.2     | ✓ graph, analyse, and compare rational functions   |
|         | ✓ determine whether graphs of rational functions have an asymptote or a point of discontinuity for a non-permissible value |
| 9.3     | ✓ relate the roots of rational equations to the x-intercepts of the graphs of rational functions                           |
|         | ✓ determine approximate solutions to rational equations graphically  |

| Assessment   | Supporting Learning  |
|--|--|
| <b>Assessment for Learning</b>   |  |
| <p><b>Method 1:</b> Use the introduction on page 428 in <i>Pre-Calculus 12</i> to activate students' prior knowledge about the skills and processes that will be covered in this chapter.</p> <p><b>Method 2:</b> Have students develop a journal entry to explain what they personally know about rational functions.</p> | <ul style="list-style-type: none"> <li>Have students update their list of what they need to work on and keep track of the skills and processes that need attention.</li> <li>Students who require activation of prerequisite skills may wish to complete <b>BLM 9–1 Chapter 9 Prerequisite Skills</b>. This material is on the Teacher CD of this Teacher's Resource and mounted on the <a href="http://www.mcgrawhill.ca/school/learningcentres">www.mcgrawhill.ca/school/learningcentres</a> book site.</li> </ul>                         |
| <b>Assessment as Learning</b>  |  |
| <p>As students work on each section in Chapter 9, have them keep track of any problems they are having.</p>  | <ul style="list-style-type: none"> <li>As students complete each section, have them review the list of items they need to work on and check off any that have been handled.</li> <li>Encourage students to write definitions for the Key Terms in their own words, including reminder tips that may be helpful for review throughout the chapter.</li> <li>Encourage students to write examples of their own in their notebook or math portfolio. Students should have an example for each method that is covered in the chapter.</li> </ul> |
| <b>Assessment for Learning</b>   |  |
| <p><b>BLM 9–1 Chapter 9 Prerequisite Skills</b><br/>This master provides a review of prerequisite skills needed for the chapter</p>  | <ul style="list-style-type: none"> <li>Use the Prerequisite Skills blackline master to provide additional opportunities for students to demonstrate their readiness for the chapter material.</li> </ul>   |

## Chapter 9 Planning Chart

| Section/<br>Suggested Timing   | Prerequisite Skills   | Materials/Technology                    | Teacher's Resource<br>Blackline Masters  | Exercise Guide  | Assessment                |                            |  | Web  <a href="http://www.mcgrawhill.ca/school/learningcentres">www.mcgrawhill.ca/school/learningcentres</a> |
|--|---|---|--|---|---------------------------|----------------------------|--|--|
|  |   |   |  |   | Assessment<br>as Learning | Assessment<br>for Learning | Assessment<br>of Learning                |  |
| <b>Chapter Opener</b><br>• 30–40 min<br>(TR page 231)  | Students should be familiar with<br>• equations and functions<br>• rational versus irrational expressions   |   | BLM 9–1 Chapter 9 Prerequisite Skills<br>BLM U4–1 Unit 4 Project Checklist   |   |                           |                            |  | • accounting careers and educational programs  |
| <b>9.1 Exploring Rational Functions Using Transformations</b><br>• 90–120 min<br>(TR page 233) | Students should be familiar with<br>• graphing, using a table of values and technology<br>• transformations<br>• factoring polynomials  | • graphing technology                   | BLM 9–2 Section 9.1 Extra Practice   | <b>Essential:</b> #1–4, 6, 8, 10, 11, 13, 16 or 18<br><b>Typical:</b> #1–3, 5–10, 12, 14 or 15, one of 16–18, C1–C3<br><b>Extension/Enrichment:</b> #5, 7, 9, 17, 19–22, C1–C3  | TR pages 235, 240         | TR pages 238, 240          |  | • tourism information about Atlin, BC  |
| <b>9.2 Analysing Rational Functions</b><br>• 60–90 min<br>(TR page 241)                        | Students should be familiar with<br>• non-permissible values<br>• asymptotes  | • graphing technology                   | BLM 9–3 Section 9.2 Extra Practice   | <b>Essential:</b> #1, 2a), b), 3, 4a), b), 5, 6a), b), 7, one of 13–15<br><b>Typical:</b> #1, 2c), d), 3, 4c), d), 6–15, one of 16–19, C1–C3<br><b>Extension/Enrichment:</b> #8, 10, 11, 16–23, C1–C3   | TR pages 242, 245         | TR pages 244, 245          |  |  |
| <b>9.3 Connecting Graphs and Rational Equations</b><br>• 90–120 min<br>(TR page 246)           | Students should be familiar with<br>• solving equations algebraically<br>• the relationship between roots and $x$ -intercepts<br>• calculating intersection points and their significance | • graphing technology                   | BLM 9–4 Section 9.3 Extra Practice   | <b>Essential:</b> #1, 2, 3a), b), 4a), b), 5, 7, 11<br><b>Typical:</b> #1, 2, 3c), d), 4c), d), 5–7, 8 or 9, 10, 12 or 13, C1–C3<br><b>Extension/Enrichment:</b> #6, 8 or 9, 10, 12 or 13, 14–17, C1–C3   | TR pages 247, 250         | TR pages 249, 250          |  | • information on the Canadian Francophone Games  |
| <b>Chapter 9 Review and Practice Test</b><br>• 60–90 min each<br>(TR page 251)                 |   | • graphing technology<br>• poster board | BLM 9–2 Section 9.1 Extra Practice<br>BLM 9–3 Section 9.2 Extra Practice<br>BLM 9–4 Section 9.3 Extra Practice<br>BLM 9–5 Chapter 9 Study Guide<br>BLM 9–6 Chapter 9 Test<br>BLM 9–7 Chapter 9 BLM Answers | Have students do at least one question related to any concept, skill, or process that has been giving them trouble.<br><b>Chapter 9 Review minimum:</b> #1–3, 4–9, 11<br>Provide students with the number of questions they can comfortably do in one class. Choose at least one question for each concept, skill, or process.<br><b>Chapter 9 Practice Test minimum:</b> #1–12 |                           | TR page 252                | TR page 252<br>BLM 9–6<br>Chapter 9 Test | • information on spill modelling   |