McGraw-Hill Ryerson

# Pre-Calculus 11 Student Workbook

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# Overview

# This McGraw-Hill Ryerson Pre-Calculus 11 Student Workbook is designed to complement the student resource.

## **Student Workbook Features for Students**

- Each section begins with Key Ideas that summarize the concepts needed to complete the exercises.
- The sections continue with working examples that guide you through the skills needed to complete the exercises.
- The working examples often include references to the *Pre-Calculus 11* student resource. These references suggest that you compare the methods used to solve the examples, or review similar examples to help consolidate your understanding of the concepts.
- Exercises are organized into three sections: Practise, Apply, and Connect.
- A selection of questions in the exercise sections include references to similar questions in the *Pre-Calculus 11* student resource.
- A review of all sections is included at the end of each chapter.
- Each chapter includes at least one Skills Organizer that assists you in summarizing the important information in that chapter.
- Answers to all questions are provided at the back of the book.
- To access Study Checks for each chapter, which will help you identify what skills and concepts you need to reinforce, go to www.mhrprecalc11.ca and follow the links to the Student Workbook.

### **Student Workbook Features for Teachers**

• For SMART Board<sup>TM</sup> lessons related to each topic, go to www.mhrprecalcl1.ca and follow the links to the Student Workbook.