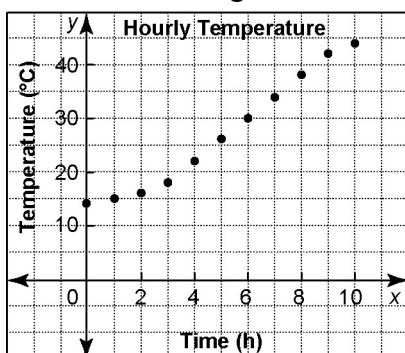


Section 7.5 Modelling Exponential Growth and Decay

- Truong studied a pond where frogs lay eggs. He found the number of tadpoles increased by a factor of 2.43 per day. The number of tadpoles, T , can be modelled by the relation $T = 265(2.43)^t$, where t is the time in days.
 - Use a graphing calculator. Graph the relation.
 - How many tadpoles were present at the start of Truong's study?
 - How many tadpoles were present after two days?
 - How many tadpoles were present after one week?
- The graph shows the temperature in a small South African village each hour for 10 h.



- After how long did the temperature increase to 20°C?
 - After how long did the temperature increase to 30°C?
 - Is it reasonable to expect that the temperature will continue to increase? Explain.
- Late in the summer, the population of black flies starts to decrease by 4% per day. The population, P , can be modelled by the relation $P = 6720(0.96)^t$, where t is the time in days.
 - Use a graphing calculator. Graph the relation.
 - What is the initial population of black flies?
 - What would be the population at the end of each of the first and second weeks?
 - Approximately how long will it take for the population to be reduced by 50%?
 - For every 5°C increase in temperature, the length of a metal bar increases by 6%. The length of the bar is 2.50 m at 10°C.
 - Make a table of values for this relation. Use increments of 5°C.
 - Use a graphing calculator to make a scatter plot of the data.
 - Find the equation of the exponential curve of best fit.
 - Use the equation to find the temperature at which the bar would be 4.00 m long.

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Date: _____

BLM 7-10
(page 2)

5. The table shows the amount remaining from a 500 mg sample of radioactive material over time.

Time (days)	Mass (mg)
0	500
1	243
2	108
3	63
4	28
5	19

- a) Use a graphing calculator. Plot the data and find the equation of the exponential curve of best fit.
- b) Use the equation to find the mass remaining after 14 days.
- c) When will there be 0.001 mg remaining?
6. The table shows the world population in billions. The year 1750 is set as $t = 0$.

Year	t	Population (billions)
1750	0	0.79
1800	50	0.98
1850	100	1.26
1900	150	1.65
1950	200	2.52
2000	250	6.06

- a) Make a scatter plot of the data. Find the equation of the exponential curve of best fit.
- b) Use the equation to estimate the population in 2050.
- c) When will the world population reach 7 billion?

7. The initial population of a bacterial culture is 2000 and the population grows at a fixed rate. The table shows the population every hour for 6 h.

Time (h)	Population
0	2000
1	2270
2	2614
3	2980
4	3392
5	3914
6	4456

- a) Use a graphing calculator. Find the equation of the exponential curve of best fit.
- b) Use the equation to find the population of bacteria after 12 h and after 24 h.
- c) How long will it take for the population to reach 20 000?
8. The populations, P , of the twin cities New Oldtown (NO) and Old Newtown (ON) can be modelled by the relations $P_{NO} = 225\,150(1.032)^t$ and $P_{ON} = 274\,500(1.026)^t$, where t is time in years since 2007.
- a) Use technology to determine the year in which the populations of the two cities will be equal.
- b) What is this population?