# 8.3

# Student Text Pages

436–441

#### Suggested Timing 80 min

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#### Tools

calculators

#### Related Resources

BLM 8-7 Section 8.3 Present Value BLM A-9 Communication General Scoring Rubric

# **Present Value**

# **Link to Get Ready**

Students should have completed **question 7** before proceeding with this section.

# Warm-Up

- Find *i*, the interest rate per compounding period, and *n*, the number of compounding periods, for each.
   a) 4% per year for 2 years, compounded semi-annually
   b) 6% per year for 5 years, compounded monthly
   c) 8% per year for 3 years, compounded quarterly
- **2.** Evaluate. Round your answers to four decimal places.

<b>a)</b> 3 <sup>-1</sup>	<b>b)</b> 1.02 <sup>-2</sup>	<b>c)</b> 1.06 <sup>-10</sup>	<b>d)</b> 1.03 <sup>-24</sup>	<b>e)</b> 200(1.04) <sup>-6</sup>
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#### Warm-Up Answers

**1. a)** i = 0.02, n = 4**b)** i = 0.005, n = 60**2. a)** 0.3333**b)** 0.9612**c)** 0.5584**d)** 0.4919

c) i = 0.02, n = 12
e) 150.0629

# **Teaching Suggestions**

• Students find Present Value a difficult concept. It is not the mathematical formula that they find difficult, but understanding when to apply it. This is often because of the language skills involved and learning a sense of time. Provide discussion and explanations to help students identify when a present value problem presents itself.

## Warm-Up

• Write the Warm-Up questions on the board or on an overhead. Have students complete the questions independently. Then, discuss the solutions as a class.

# **Section Opener**

• Ask the students to read the opener. Ask them what they would do: would they pay the \$2399.99 now or take the installment plan?. Have them record their answers, along with a rationale. Tell them they will return to this problem after the lesson.

## Investigate

• This Investigate is important to help students understand growth factors, before applying them to compound interest and present value.

#### Investigate Answers (pages 436-437)

- a) 1, 2, 4, 8, 16, 32, 64
   b) 2
   a) 8, 12, 18, 27, 40.5, 60.75, 91.125, 136.6875
   b) 1.5
   a) 3
- **b)** 1458, 486
  - **c)** Divide the term 4374 by the growth factor 3 to get 1458. Repeat this step to get the second previous term.
- 4. a) By repeatedly dividing the growth factor 5, I can find the previous terms.b) 1875, 375

#### **Examples**

- Remind students of the meanings of *i* and *n*. Go through the development of the present value formula. You may wish to use an example, such as Example 1 to illustrate the derivation of the formula. Comment that time is negative in the formula because, when finding the present value, we are working backwards in time.
- The Examples illustrate that investments and debts both use the same formula. Stress that one person's debt is another person's investment.

#### **Key Concepts**

• Review the formulas for amount and present value. Ask the students to relate each formula to a direction on the time line.

#### **Discuss the Concepts**

- **Question D1** is a good literacy question, getting students to explain *amount* and *principal* in their own words. Have students work in pairs to complete the question.
- **Question D4** gives an opportunity to discuss the opening TV advertisement more fully.

#### Discuss the Concepts Suggested Answers (page 439)

- **D1.** *Amount* is the money value received or paid at the end of a term, while *principal* is the beginning value.
- **D2.** Principal will have a smaller value (assuming the interest rate is positive), since  $A = P(1 + i)^n$ .
- **D3.** Answers may vary. Sample answer: the value of *i* is  $6\% \div 4$  or 0.015, *n* is  $4 \times 2$  or 8. Try successive guesses for *P* in  $A = P(1.015)^8$  until the value A = 4000 is obtained. Since the interest rate is small, the principal will not grow much in 2 years. You might try 3500 as the first guess for *P*. Alternatively, use the PV formula with A = 4000, i = 0.015, and n = 8. Key in  $4000 [\times] 1.015[y^x] 8 [=]$ . The answer obtained is \$3550.84.
- **D4.** Answers may vary. Sample answer: Interest rates and payment periods should be taken into consideration.

#### Practise (A)

• Questions 1 to 3 are important to consolidate learning of the basic concepts.

#### **Common Errors**

- Some students may not understand why the exponent is negative on the present value formula.
- R<sub>x</sub> If the derivation of the formula does not help, explain that working backwards in time is like going from right to left on the time line. In other words, moving on a number line in the negative direction.

#### Accommodations

**Perceptual**—provide a handout with colour-coded compounding period information

**Language**—encourage students to work in partners for reading support

#### Apply (B)

- Instruct students to look at their answers and determine, through estimation, whether their answers are reasonable.
- Remind students that the present value must be less than the amount.
- **Question 9** links to the Chapter Problem. It is a good ongoing case study of a family's investments. Remind students to keep the solution to this question handy as the methods they used may help them with the Chapter Problem Wrap-Up.

#### Extend (C)

- Assign the Extend questions to students who are not being challenged by the questions in Apply.
- In **question 14**, students will need to find the final amount at 4.2% and the present value of that amount at 4.8%.

#### **Mathematical Process Expectations**

Process Expectation	Questions
Problem Solving	10–16
Reasoning and Proving	10, 16
Reflecting	n/a
Selecting Tools and Computational Strategies	1–16
Connecting	n/a
Representing	n/a
Communicating	n/a

#### **Ongoing Assessment**

• Assess students' mathematical communication. You may wish to use **BLM A-9 Communication General Scoring Rubric** to assist you.

#### **Extra Practice**

• You may wish to use **BLM 8-7 Section 8.3 Present Value** for remediation or extra practice.