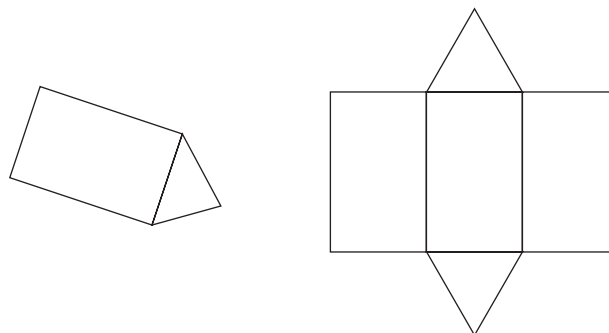


## 7.2 Surface Area of Three-Dimensional Objects

### KEY CONCEPTS

- There are a number of real-world applications involving the surface area of three-dimensional objects.
- The surface area of a three-dimensional object is the sum of the areas of all the outer faces of the object.
- Nets can be used to help visualize the faces of a three-dimensional object. A net is a two-dimensional drawing that shows the object “unfolded” so all its surfaces are visible.



### Example

You have been commissioned to design a door for a washing machine. The door of the washing machine will be a square that measures 22 in. by 22 in. with an area cut out for a circular window with diameter 8 in. The depth of the door is 3 in. Determine the surface area of the door of the washing machine to the nearest tenth of a square inch.

### Solution

Calculate the total area of the front and the back of the door.

$$\begin{aligned}A &= 2s^2 \\ &= 2 \times 22^2 \\ &= 968\end{aligned}$$

Calculate the area of the four outside edges of the door.

$$\begin{aligned}A &= 4(\ell \times w) \\ &= 4(22 \times 3) \\ &= 4 \times 66 \\ &= 264\end{aligned}$$

Calculate the area of the circular window. The diameter of the window is 8 in., so the radius is 4 in.

$$\begin{aligned}A &= \pi r^2 \\ &= \pi(4)^2 \\ &= 50.265\dots\end{aligned}$$

Calculate the circumference of the edge around the window.

$$\begin{aligned}C &= 2\pi r \\ &= 2 \times \pi \times 4 \\ &= 25.132\dots\end{aligned}$$

Calculate the area of the edges around the window.

$$\begin{aligned}
 SA &= C \times \text{depth} \\
 &\doteq 25.132 \times 3 \\
 &\doteq 75.40
 \end{aligned}$$

Calculate the total surface area of the washing machine door.

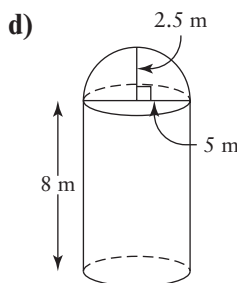
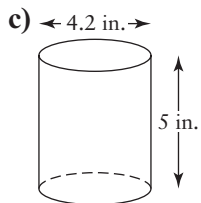
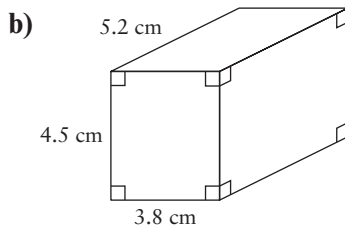
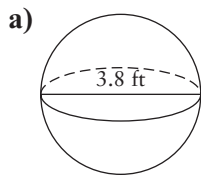
$$\begin{aligned}
 A &= A_{\text{front and back of door}} - 2A_{\text{window}} + A_{\text{around four edges}} + A_{\text{around window}} \\
 &\doteq 968 - 2(50.27) + 264 + 75.40 \\
 &\doteq 1206.86
 \end{aligned}$$

The total surface area of the washing machine door is approximately 1206.9 in.<sup>2</sup>.

### A

*Unless otherwise specified, round all measures to the nearest tenth of a unit.*

1. Calculate the surface area of each shape.



2. A box has length 15 cm, width 12 cm, and height 7 cm.
- Draw and label a net for the box.
  - Calculate the surface area of the box.
3. A closed cylindrical storage container has diameter 7.5 cm and height 11 cm.
- Calculate the surface area of the container.
  - The material used to make the container costs \$0.44 per square inch. What is the cost of material needed to make 10 containers?
  - How would the formula to calculate the surface area change if the storage container did not have a lid?
4. A cabinet is in the shape of a cube. It has surface area 6144 in.<sup>2</sup>. Determine the area of one face, and then the length of one edge of the cabinet.

### B

5. A candle is in the shape of a cylinder. It has diameter 3 in. and surface area 70.7 in.<sup>2</sup>.
- Determine the height of the candle.
  - If the candle has burned down to half its height, will the surface area be halved? Explain your reasoning.

★6. The surface area of a beach ball is  $2827 \text{ cm}^2$ . Calculate the diameter of the beach ball.

7. A storage box is in the shape of a square-based rectangular prism. The side lengths of the base are 2.5 ft and the height of the prism is 3.5 ft.
- Draw a diagram of the storage box.
  - Determine the surface area of the storage box.
  - If the dimensions of the storage box are doubled, determine the surface area of the storage box. By what factor did the surface area increase? Explain.
  - If the dimensions of the storage box are tripled, determine the surface area of the storage box. By what factor did the surface area increase? Explain.

8.
  - Determine the surface area of Sphere A with diameter 7 in.
  - The diameter of Sphere B is double that of Sphere A. Calculate the surface area of Sphere B.
  - How do the surface areas of Spheres A and B compare?
  - The diameter of Sphere C is half that of Sphere A. Predict the relationship between the surface areas of Sphere C and Sphere A. Explain your prediction.
  - Calculate the surface area of Sphere C. Compare the result to your answer to part d).

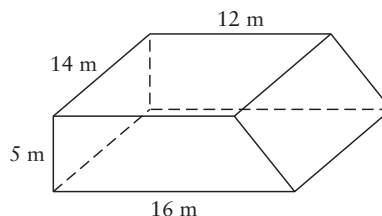
9. A rectangular piece of insulation is 40 cm long by 25.5 cm wide. It is to fit over a section of cylindrical pipe that is 40 cm long and 8 cm in diameter. Will the piece of insulation cover the section of pipe? Explain.

★10. Reid made a wooden bowl of uniform thickness that is in the shape of a hemisphere. At the top of the bowl, the outer diameter is 30 cm and the inner diameter is 28 cm.

- Determine the area of exposed wood on the outside of the bowl.
- Determine the area of exposed wood on the inside of the bowl.
- Determine the area of exposed wood on the rim of the bowl.
- One bottle of finishing oil covers  $1800 \text{ in.}^2$ . What percent of a bottle is required to coat all the surfaces of the bowl?

11. A length of rubber hose is 150 cm long. It has outer diameter 4 cm and inner diameter 3.5 cm. Determine the area of exposed rubber (inside the hose, outside the hose, and at the ends).

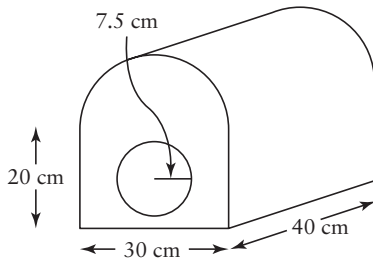
12. Mary designed a riser for a concert. The side and top faces will be painted blue.



- Sketch a net of the riser.
- Determine the area of the riser to be painted blue.

13. A cylindrical container is designed to hold three stacked tennis balls. The height of the container is 20.6 cm. A tennis ball has diameter 2.7 in. Determine the amount of material required for the cylindrical container, to the nearest square inch.

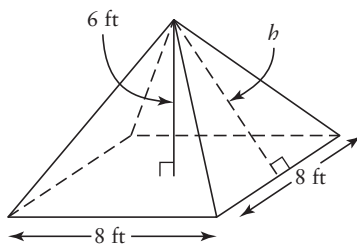
14. Ed designed a birdhouse in the shape of a rectangular prism topped by half a cylinder. The rectangular prism is 40 cm long, 30 cm wide, and 20 cm high. There is a circular hole with radius 7.5 cm cut out of the front.



- Determine the surface area of the birdhouse in square centimetres.
  - Determine the surface area of the birdhouse in square feet.
  - Explain how you determined the surface area of the birdhouse.
15. Erik is manufacturing umbrella stands. Each stand is in the shape of a cube with side lengths 2.5 ft. He drills a hole with diameter 1 ft through the centre of the top to hold umbrellas. Determine the surface area of one umbrella stand.

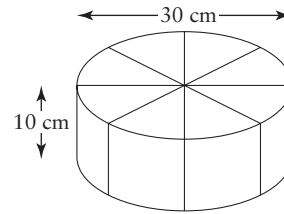
### C

16. A tent is in the shape of a square-based pyramid with side lengths 8 ft and height 6 ft.



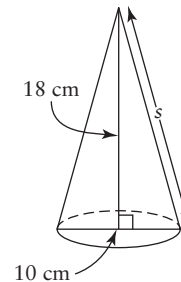
- Consider the triangular faces. Calculate the height,  $h$ , of one face.
- Determine the surface area of the tent.

17. A cylindrical wheel of cheese is cut into 8 congruent pieces.

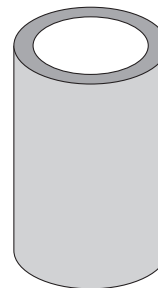


What is the least amount of wrapping required for each wedge of cheese?

18. Rae designed a candle that is in the shape of a cone. The bottom diameter is 10 cm and the height is 18 cm.



- Determine the slant height,  $s$ , of the side of the candle.
  - Determine the surface area of the candle.
  - Determine the surface area of the candle when it has burned to half its original height.
19. An open-top silo has cylindrical walls with outside diameter 5.2 m, thickness 52 cm, and height 12 m.



A can of paint costs \$15.98 and covers  $14 \text{ m}^2$ . How much will it cost to paint the silo, including the inside, the outside, and the top of the walls?