

CHAPTER 17	Determining $K_a$ and Percent Ionization	BLM 17.3.1
OVERHEAD		

### Problem

Propanoic acid,  $\text{CH}_3\text{CH}_2\text{COOH}(\text{aq})$ , is a weak monoprotic acid that is used to inhibit mould formation in bread. A student prepared a 0.10 mol/L solution of propanoic acid and found the pH was 2.96. What is the acid ionization constant for propanoic acid? What percentage of its molecules were ionized in the solution?

### What Is Required?

You need to find  $K_a$  and the percent ionization for propanoic acid.

### What Is Given?

You have the following data:

Initial  $[\text{C}_2\text{H}_5\text{COOH}(\text{aq})] = 0.10 \text{ mol/L}$

pH = 2.96

### Plan Your Strategy

**Step 1** Write the equation for the ionization equilibrium of propanoic acid in water. Then set up an ICE table.

**Step 2** Write the expression for the acid ionization constant.

**Step 3** Calculate  $[\text{H}_3\text{O}^+(\text{aq})]$  using  $[\text{H}_3\text{O}^+(\text{aq})] = 10^{-\text{pH}}$ .

Note that  $[\text{C}_2\text{H}_5\text{COO}^-] = [\text{H}_3\text{O}^+]$ .

**Step 4** Use the stoichiometry of the equation and  $[\text{H}_3\text{O}^+(\text{aq})]$  to complete the ICE table. Calculate  $K_a$ .

**Step 5** Calculate the percent ionization by expressing the fraction of molecules that ionize out of 100.

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### Act on Your Strategy

**Step 1** Use the equation for the ionization equilibrium of propanoic acid in water to set up an ICE table.

	$\text{C}_2\text{H}_5\text{COOH}(\text{aq}) + \text{H}_2\text{O}(\ell) \leftrightarrow \text{C}_2\text{H}_5\text{COO}^-(\text{aq}) + \text{H}_3\text{O}^+(\text{aq})$			
	$[\text{C}_2\text{H}_5\text{COOH}(\text{aq})]$ (mol/L)	$[\text{H}_2\text{O}(\ell)]$ (mol/L)	$[\text{C}_2\text{H}_5\text{COO}^-(\text{aq})]$ (mol/L)	$[\text{H}_3\text{O}^+(\text{aq})]$ (mol/L)
Initial	0.10		0	~0
Change	$-1.1 \times 10^{-3}$		$+1.1 \times 10^{-3}$	$+1.1 \times 10^{-3}$
Equilibrium	$0.10 - 1.1 \times 10^{-3}$		$1.1 \times 10^{-3}$	$1.1 \times 10^{-3}$

**Step 2** Remember, pure water is not included in the expression for  $K_a$ .

$$K_a = \frac{[\text{C}_2\text{H}_5\text{COO}^-][\text{H}_3\text{O}^+]}{[\text{C}_2\text{H}_5\text{COOH}]}$$

**Step 3** Calculate the value of  $[\text{H}_3\text{O}^+(\text{aq})]$ .

$$[\text{H}_3\text{O}^+(\text{aq})] = 10^{-\text{pH}}$$

$$[\text{H}_3\text{O}^+(\text{aq})] = 10^{-2.96}$$

$$[\text{H}_3\text{O}^+] = 1.1 \times 10^{-3} \text{ mol/L}$$

**Step 4** Recall that  $[\text{C}_2\text{H}_5\text{COO}^-] = [\text{H}_3\text{O}^+]$

$$K_a = \frac{(1.1 \times 10^{-3})^2}{0.10 - (1.1 \times 10^{-3})}$$

$$= 1.2 \times 10^{-5}$$

**Step 5**

$$\text{Percent ionization} = \frac{1.1 \times 10^{-3} \frac{\text{mol}}{\text{L}}}{0.10 \frac{\text{mol}}{\text{L}}} \times 100\%$$

$$= 1.1\%$$

### Check Your Solution

The value for  $K_a$  and the percent ionization are reasonable for a weak acid.

### MathTip

As you know, powers of ten do not count in the number of significant digits in a measurement. For this reason, the part of a logarithm that depends on the power of ten does not count in the number of significant digits in the logarithm. For example, the number  $3.57 \times 10^4$  has three significant digits. The logarithm of  $3.57 \times 10^4$  is 4.5527. The numeral 4 to the left of the decimal represents the exponent of 10, so it does not count in the number of significant digits. The numerals to the right of the decimal determine the 3.57, so they count as significant digits. (**Hint:** Find the logarithm of  $3.57 \times 10^8$ .) Therefore, the logarithm of  $3.57 \times 10^4$  with the correct number of significant digits is 4.553. If the concentration of hydronium ion is  $1.1 \times 10^{-5} \text{ mol/L}$ , there are two significant digits. The pH is 4.96, correct to two significant digits.