

# Principles of Mathematics 9:

## Teacher's Resource

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## Blackline Masters

### (Available on *Principles of Mathematics 9: Teacher's Resource CD-ROM*)

This package has generic masters, generic assessment masters, and student success masters, along with chapter-specific worksheets, assessment tools, and technology masters.

Blackline Masters are provided in WORD and PDF format for each skill reviewed on the Get Ready pages, and for each numbered section of the text. A Chapter Test is provided for each chapter. Answers are given for all these extra questions.

The BLM package also includes rubrics for the chapter problem wrap-ups and chapter tasks, chapter test assessment masters, and chapter mark summaries. These will assist you in keeping track of student achievement by chapter, strand, and category.