

BLM Answers

BLM 7.GR.3 Practice: Get Ready

- equilateral triangle
 - isosceles triangle
- right isosceles triangle
 - obtuse scalene triangle
- irregular; rectangle
 - irregular; trapezoid
 - regular; square
- regular; pentagon
 - irregular; hexagon
 - irregular; triangle
- $x = 81^\circ$
 - $x = y = z = 60^\circ$
- $a = 135^\circ; b = 45^\circ; c = 45^\circ$
 - $a = 105^\circ; b = 75^\circ; c = 105^\circ$

BLM 7.1.1 Practice: Angle Relationships in Triangles

- 115°
 - 116°
 - 111°
 - 120°
 - 55°
 - 85°
- 138°
 - 130°
 - 61°
 - 123°
 - 143°
 - 90°
- 105°
 - 145°
 - 124°
 - 110°
- $x = 95^\circ$
 - $x = y = 55^\circ; z = 70^\circ$
 - $x = 50^\circ; y = 115^\circ; z = 130^\circ$
 - $x = 45^\circ; y = 15^\circ; z = 30^\circ$
- $138^\circ, 138^\circ, 84^\circ$ or $138^\circ, 111^\circ, 111^\circ$

BLM 7.1.3 Word Origins and Plurals

Word	Origin	Plural
1. Appendix	Latin	appendices
2. Minimum	Latin	minima
3. Matrix	Latin	matrices
4. Radius	Latin	radii
5. Polyhedron	Greek	polyhedra
6. Focus	Latin	foci
7. Index	Latin	indices
8. Formula	Latin	formulae
9. Datum	Latin	data
10. Basis	Latin and Greek	bases
11. Hypothesis	Latin and Greek	hypotheses
12. Analysis	Latin and Greek	analyses

BLM 7.2.1 Angle Relationships in Quadrilaterals

- 110°
 - 86°
 - 120°
 - 125°
- 146°
 - 73°
 - 93°
 - 65°
- 95°
 - 20°
 - 160°
 - 113°
- 125°
 - 80°
 - 72°
 - 63°

- $x = y = 85^\circ$
 - $x = 130^\circ; y = 50^\circ$
 - $x = y = 145^\circ; z = 35^\circ$
 - $x = z = 105^\circ; y = 75^\circ$
- $x = 90^\circ; y = 53^\circ$
 - $a = 140^\circ; b = 52^\circ$
 - $m = 25^\circ; n = 155^\circ; p = 25^\circ$
 - $s = 85^\circ; t = 50^\circ; v = 108^\circ; x = 63^\circ; y = 72^\circ$

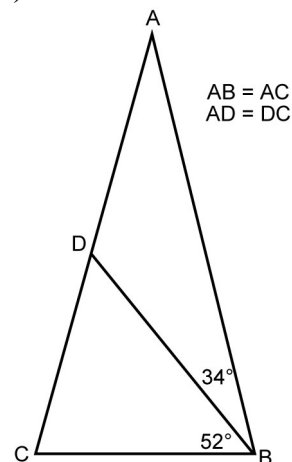
BLM 7.3.1 Practice: Angle Relationships in Polygons

- 540°
 - 360°
 - 900°
 - 1260°
- 1440°
 - 720°
 - 360°
 - 1080°
- 1620°
 - 2160°
 - 2880°
 - 3960°
- 60°
 - 162°
 - 140°
 - 157.5°
- 6 sides
 - 13 sides
 - 15 sides
 - 25 sides

BLM 7.4.1 Practice: Midpoints and Medians in Triangles

- 31 m
 - 1.5 cm
 - 54 cm
 - 4 m
- AD = 15 m; DE = 20 m
 - AD = 4 cm; DE = 5.8 cm
 - AD = 60 m; DE = 104 m
 - AD = 6 cm; DE = 13.2 cm
- 5 cm^2
 - 5 cm^2
- 24 cm^2
 - 12 cm^2
- The median divides the isosceles triangle into two smaller triangles. It bisects the unequal side, and is a common side in each of the smaller triangles. The original triangle is isosceles, so the third sides in the smaller triangles are equal. The angles opposite the new common side were equal and still are, and both new triangles have a right angle where the common side meets the original unequal side. Therefore, the two triangles have all sides equal and two angles equal, so the third angle in each must be equal. So, the median to the vertex opposite the unequal side of an isosceles triangle bisects the angle at that vertex.

b) False



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BLM 7.4.3 Sierpinski's Triangle

- equidistant from the endpoints of the original line segment.
- a) Call the school at (1, 9) school A, the school at (3, 2) school B, and the school at (9, 5) school C.

Using the method of finding the equation of a line using two points, the equation of the line AB is

$$y = \left(\frac{-7}{2}\right)x + \frac{25}{2}. \text{ Similarly the equation for line}$$

$$\text{BC is } y = \left(\frac{1}{2}\right)x + \frac{1}{2}, \text{ and the equation of line AC}$$

$$\text{is } y = \left(\frac{-1}{2}\right)x + \frac{19}{2}.$$

We know that the slope of the perpendicular bisector of a line is the inverse reciprocal of the slope of the original line. Using this, we can find the slopes of the perpendicular bisectors of lines AB, BC, and AC.

The midpoints of lines AB, BC, and AC are

$$\left(\left(\frac{1+3}{2}\right), \left(\frac{9+2}{2}\right)\right) = \left(2, \frac{11}{2}\right), \left(6, \frac{7}{2}\right), \text{ and}$$

(5, 7) respectively.

Using the slope and one point method of finding the equation of a line, we can find the equations of the perpendicular bisectors.

$$\text{Perpendicular bisector of line AB is } y = \left(\frac{2}{7}\right)x + \frac{69}{14}$$

$$\text{Perpendicular bisector of line BC is } y = -2x + \frac{31}{2}$$

$$\text{Perpendicular bisector of line AC is } y = 2x - 3.$$

These are the equations of the boundaries between schools A and B, B and C, and A and C respectively, since the points on these lines are equidistant from each pair of schools.

- b) Graphing these lines, we see that they all intersect at a point roughly (4.5, 6.25), the point equidistant from all three schools. Solving any two of the equations as a system, we find the actual intersection point

$$\left(\frac{37}{8}, \frac{25}{4}\right) \text{ or } (4.6, 6.25).$$

- The boundaries between the original three schools still apply. We just need boundaries between new school D and each of the original three.

By the same methods as above, the equation for

$$\text{CD is } y = \left(\frac{-5}{2}\right)x + \frac{55}{2}, \text{ the equation for AD is}$$

$$y = \left(\frac{1}{6}\right)x + \frac{53}{6}, \text{ and the equation for BD is}$$

$$y = 2x - 4.$$

$$\text{The perpendicular bisectors are } y = \left(\frac{2}{5}\right)x + \frac{43}{10},$$

$$y = -6x + \frac{67}{2}, \text{ and } y = \left(\frac{-1}{2}\right)x + \frac{17}{2}.$$

The boundaries between each pair of schools is

$$y = \left(\frac{2}{7}\right)x + \frac{69}{14}$$

$$y = -2x + \frac{31}{2}$$

$$y = 2x - 3$$

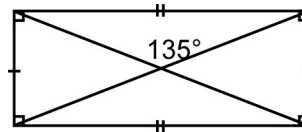
$$y = \left(\frac{2}{5}\right)x + \frac{43}{10}$$

$$y = -6x + \frac{67}{2}$$

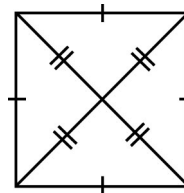
$$y = \left(\frac{-1}{2}\right)x + \frac{17}{2}$$

BLM 7.5.2 Practice: Midpoints and Diagonals in Quadrilaterals

- AB and DC; AD and BC
 - AD and BC; AB and DC
- $x = z = 127^\circ; y = 53^\circ$
 - $q = s = 65^\circ; t = 115^\circ$
- 3.6 cm b) 7.2 cm c) 6 cm d) 12 cm
- 6.6 cm b) 6.6 cm c) 6.6 cm d) 13.2 cm
- False



- b) True



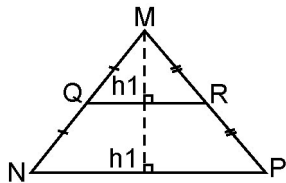
The diagonals and the sides of the square form four congruent isosceles triangles. The angles formed by the equal sides of the triangles are all equal, so the four angles in the middle must be equal. The sum of the measures of these angles is 360° . The measure of each angle is $360 \div 4$, or 90° .

BLM 7.CR.1 Chapter 7 Review

- $x = 135^\circ$ b) $x = 108^\circ$
 - $x = 121^\circ$ d) $x = 62^\circ; y = 112^\circ; z = 118^\circ$
- $48^\circ; 72^\circ; 156^\circ; 132^\circ$

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3. a) $a = 138^\circ$ b) $k = 68^\circ$
 c) $x = z = 130^\circ; y = 50^\circ$
 d) $a = c = 150^\circ; b = d = 30^\circ$
4. a) 157° b) $159^\circ, 86^\circ, 92^\circ, 23^\circ$
5. a) 540° b) 1440° c) 360° d) 900°
6. a) 60° b) 120° c) 135° d) 144°
7. 20
8. a) 32 cm^2 b) 16 cm^2
9. a) True



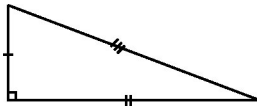
The area of $\triangle MQR$ is $\frac{1}{2}QR \times h$.

The area of $\triangle MNP$ is $\frac{1}{2}NP \times 2h$ or $NP \times h$.

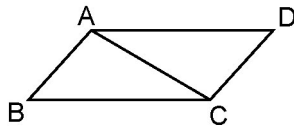
But $NP = 2 \times QR$.

So, the area of $\triangle MNP$ is $2 \times QR \times h$.

- b) False



10. a) WZ and XY; WX and ZY
 b) DE and GF; DG and EF
11. a) True



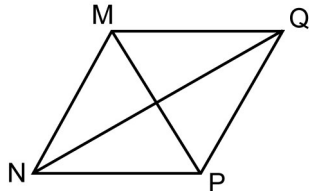
$$AB = DC$$

$$BC = AD$$

$$AC = AC$$

So, $\triangle ABC$ is congruent to $\triangle CDA$.

- b) False



$$NQ = 5.2 \text{ cm}$$

$$MP = 3 \text{ cm}$$

BLM 7.PT.1 Chapter 7 Practice Test

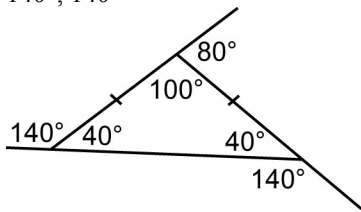
1. D
 2. B
 3. D
 4. C
 5. A
 6. a) $x = 21^\circ$
 b) $x = 32^\circ$
 c) $a = 70^\circ; b = 40^\circ; c = e = 110^\circ; d = 140^\circ$
 d) $m = p = q = 125^\circ; n = r = s = 55^\circ$
7. 3240°
8. a) True; three diagonals can be drawn from one vertex of a hexagon. These diagonals divide the hexagon into four triangles. The sum of the interior angles of a triangle is 180° . Since there are four triangles in a hexagon, the sum of the interior angles is 4×180 , or 720° .
 b) False; the sum of the exterior angles of any convex polygon is always 360° .
9. a) 8 b) 135°
10. The area of BCED is $\frac{(DE + BC) \times BD}{2}$.
 But $BC = 2DE$.
 So, the area becomes $\frac{(DE + 2DE) \times BD}{2}$ or $\frac{3DE \times BD}{2}$.
 The area of $\triangle ADE$ is $\frac{DE \times AD}{2}$.
 But $AD = BD$.
 So, the area becomes $\frac{DE \times BD}{2}$.

BLM 7.CT.1 Chapter 7 Test

1. B
 2. C
 3. B
 4. D
 5. C
 6. a) $x = 53^\circ$ b) $x = 145^\circ$
 c) $x = y = z = 60^\circ; a = b = c = 120^\circ$
 d) $a = 126^\circ; b = 131^\circ; c = 110^\circ; d = 147^\circ; e = 49^\circ$
7. 1260°
8. a) False; the sum of the interior angles of a triangle is 180° . If two angles are obtuse, the sum of the angles will be greater than 180° .
 b) True; the sum of the interior angles of a quadrilateral is 360° . A quadrilateral can have one or two obtuse angles.

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9. a) 157.5° b) 22.5°
10. a) $140^\circ, 140^\circ$



- b) One; if the 80° exterior angle is at one of the vertices with equal interior angles, the equal interior angles would be 100° . The sum of the interior angles of a triangle is 180° . $2 \times 100^\circ = 200^\circ$, so this triangle is not possible.