

Combining Percents

MathLinks 8, pages 144–149

Suggested Timing

80-100 minutes

Materials

- sample advertisements featuring percent-off sales
- base ten blocks or hundred grids (optional)
- calculator

Blackline Masters

Master 10 Hundred Grids BLM 4–3 Chapter 4 Warm-Up BLM 4–12 Section 4.4 Extra Practice BLM 4–13 Section 4.4 Math Link

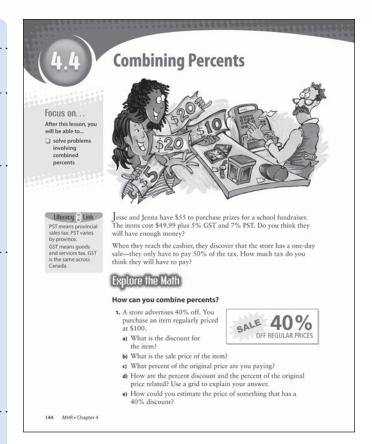
Mathematical Processes

- Communication (C)
- Connections (CN)
- Mental Mathematics and Estimation (ME)
- Problem Solving (PS)
- 🖌 Reasoning (R)
- 🖌 Technology (T)
- ✓ Visualization (V)
-

Specific Outcomes

N3 Demonstrate an understanding of percents greater than or equal to 0%.

Category	Question Numbers
Essential (minimum questions to cover the outcomes)	1–4, 6, 8, 10, Math Link
Typical	1-4, 6, 8-12, Math Link
Extension/Enrichment	1-3, 13, 14, Math Link



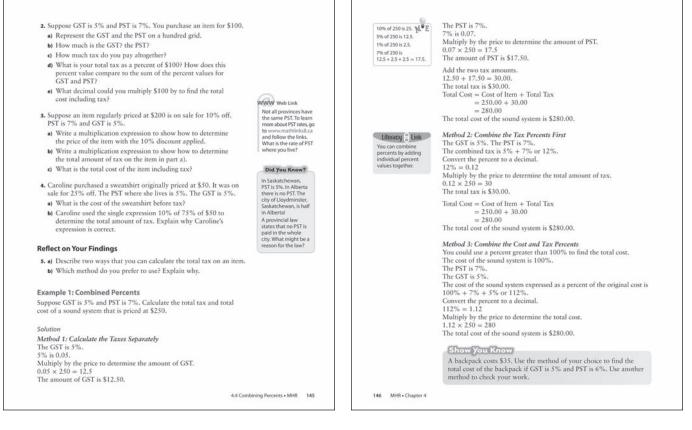
Planning Notes

Have students complete the warm-up questions on **BLM 4–3 Chapter 4 Warm-Up** to reinforce material learned in previous sections.

As a class, read and discuss the scenario. Since many problems involving combined percents and percents of percents are connected with consumer events such as taxes and percent-off sales, consider showing and discussing some sample advertisements highlighting these features. Look for ads that make claims such as "We pay the tax!" or "20 percent off already discounted items."

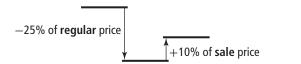
Ask students to predict whether Jesse and Jenna will have enough money. Consider having students test their prediction after covering the content of section 4.4.

Literacy Link As a class, read the Literacy Link on page 144 and have students identify the PST rate (if applicable) and the GST rate where they live.



Explore the Math

In this exploration, students are introduced to combining percents in the context of consumer purchases. Students are led through multiple steps that should lead to an understanding of the impact of combined percents. Note that in #4, many students may think that 25% off together with 10% added on must be the same as 15% off. This is a difficult concept. Explain that 25% off and 10% added on represent percents of different wholes, and that percents of different wholes cannot be combined. Consider using the following visual representation to help foster understanding:



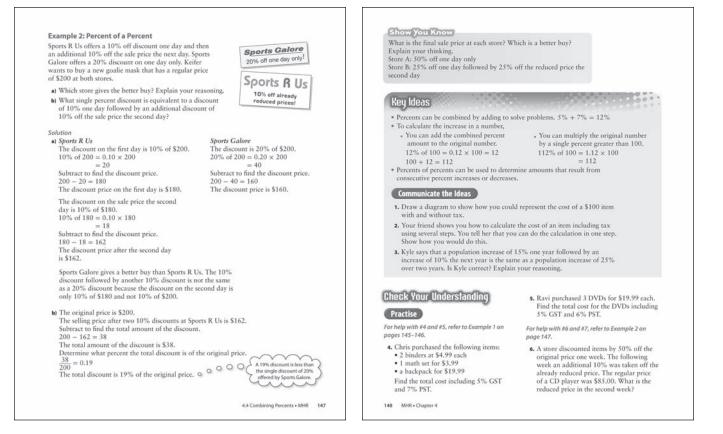
♦25% and **♦**10% is *not* equal to **♦**15%.

Explain that the values (in the example) cannot be combined into a single percent because they represent percents of different numbers. Have students discuss their findings as a class. **Method 1** Have students work in pairs on all questions. Discuss the answers as a class. Have students consider and list the different methods for calculating tax, decide which method they prefer, and provide justification.

Method 2 Make the questions concrete by bringing in actual items or pictures of items that cost close to the prices suggested and putting sales notes, PST rates, and GST rates on them. Divide the class into two large groups. Have one group work on #1 and the second work on #2. When the group members have completed the two questions, have the team members coach members of the other group in how to do that type of question.

- Encourage students to use visuals to show how they know their answer is correct and to suggest some mental math and estimation techniques that might help in solving or checking the reasonableness of answers.
- Encourage students to show more than one way to do the calculations.
- Use the same teams to solve #3 and #4, and then share their solutions and methods.

As a class, discuss the findings. Have students consider and list the different methods for calculating tax, decide which method they prefer, and provide justification.



Example 1

Example 1 demonstrates three methods for solving a combined tax problem: calculating the taxes separately, combining the tax percents first, and combining the cost and tax percents. Discuss each method with students. Have them consider the similarities and differences. Emphasize checking answers by doing a question using one method, then checking it using the second. Also have students use mental math techniques for checking the reasonableness of answers.

Literacy Link Direct students to the Literacy Link on page 146 that explains what a combined percent is. Combining percents can be helpful when estimating the cost of an item after tax.

Consider breaking the class into groups of three to do the Show You Know. Have students in each group use a different method and then compare answers.

Example 2

Example 2 demonstrates how to find the final sale price of an item whose price changes in two ways in competing stores. Use the visual on page 147 to demonstrate why Sports Galore has the better buy.

Meeting Student Needs

• For #4b), you may need to explain the expression 10% of 75% of \$50 to students. Explain that Caroline is paying 11% combined tax on the sale price of the sweatshirt. The sweatshirt costs 75% of its original price (\$50). You may need to show this visually using one or more hundred grids.

ELL

- English language learners may benefit from making a list of terms associated with money, such as *discount, additional discount off the sale price, original price, total discount, final sale price,* and 25% off the reduced price. Have them write the meaning of each term. As a class, discuss the meaning of each term and then have students make revisions, if necessary, before adding the notes about the terms to section 4.4 in their chapter Foldable.
- English language learners may have difficulty with terms such as *purchase*, *backpack*, and *goalie mask*. Have students add any new terms to their dictionary.

Gifted and Enrichment

• Have students access the Web Link on page 145 in the student resource and compare PST rates across Canada. Encourage them to speculate about why PST rates may differ from province to province. • Challenge students to research why no PST is paid in Lloydminster (provincial sales tax exemption is intended to level the playing field for businesses on the Saskatchewan side of Lloydminster).

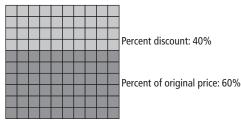
Common Errors

- Some students may incorrectly convert a percent to a decimal.
- **R**_x Remind students to convert a percent to a decimal by dividing by 100, so that 20% is 0.20, not 20.0.

Answers

Explore the Math

- **1.** a) \$40 b) \$60 c) 60%
 - **d)** The sum of the percent discount and percent of the original price add to 100%.



e) Calculate 50% of the original price, then add 10% of the original price.

c) \$12

2. a) GST

051										
								F	PST	

d) 12%; The total tax as a percent is equal to the sum of the percent rates for the PST and GST.e) 1.12

b) GST: \$5; PST: \$7

- **3.** a) 200×0.9 b) $1.12 \times 200 \times 0.9$ c) \$201.60
- 4. a) \$37.50
 - **b)** 75% of \$50 represents the cost after the discount before tax. Then calculating 10% of the discounted price represents the combined PST and GST tax rates.
- **5.** a) For the first method, calculate the PST and GST taxes separately, and then add them together. For the second method, combine the GST and PST tax rates, as percents, and then use this combined rate to calculate the total tax.
 - **b)** Answers will vary. Example: I prefer the second method because it is easier to add the two tax rates, as percents, than it is to add the amounts of these two taxes in monetary values.

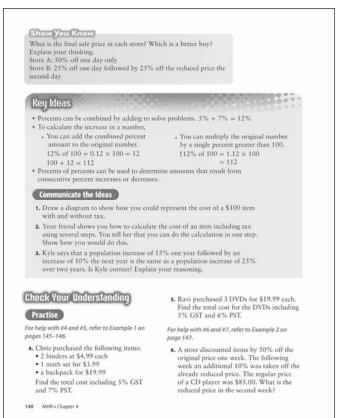
Show You Know: Example 1

Look for one method to determine the total cost and a second method to verify the answer, which is \$38.85.

Show You Know: Example 2

Store A: 50% discount; Store B: 43.75% discount; Store A is offering a better deal.

Assessment	Supporting Learning
Assessment as Learning	
Reflect on Your Findings Listen as students discuss what they discovered during the Explore the Math. Try to have students generalize the conclusion about their findings.	 For #2, encourage students who struggle with numeracy to combine the cost of the item and the taxes in one multiplication process. For example, they could multiply by 1.12, where the taxes are 5% and 7%, respectively. For #2e), students may need prompting to discover the idea that they need to multiply by 112%. For #4, most students may need prompting to discover the idea that 25% off means that 75% remains. This can be shown visually on a hundred grid. Have students record different ways of estimating the total cost of an item including taxes. Have students verbalize the process and then add their notes to their chapter Foldable.
Assessment for Learning	
Example 1 Have students do the Show You Know related to Example 1.	 Encourage students to verbalize their thinking. You may wish to have students work with a partner. Some students may need to be coached through the process of changing a percent to a decimal and may benefit from using a calculator. Give students a similar problem to solve. Allow them to work with a partner and talk through their thinking. Have students share any different methods they have for finding the final sale price of an item including taxes. Have them add any additional methods to their chapter Foldable.
Example 2 Have students do the Show You Know related to Example 2.	 Encourage students to verbalize their thinking. You may wish to have students work with a partner. Give students a similar problem to solve. Allow them to work with a partner and talk through their thinking.



Communicate the Ideas

These questions allow students to show their understanding of combining percents and percents of percents. In #1, students draw a diagram to represent combining percent. In #2, they calculate the cost of an item in one step. In #3, students explain why percents of different population sizes cannot be combined. Have students share their answers for #3 in a class discussion.

Meeting Student Needs

• Students may need to be reminded that the value 112% converts to 1.12 as a decimal.

ELL

• Explain the term *population increase* using an example of a local animal population with which students may be familiar.

Answers

Communicate the Ideas

1. Answers will vary. Example:

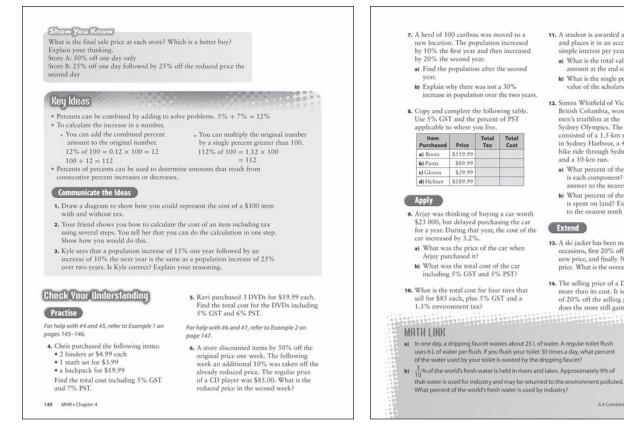
Со	Cost of an item without tax								

- **2.** Mentally combine the tax rates with 100%. If the tax rates sum to 12%, then add this to 100%, which represents the cost of the item before taxes. Simply multiply the cost of the item by 112% as a decimal. For example, if the cost of the item is \$200, then the single calculation is $1.12 \times $200 = 224 .
- **3.** No, Kyle is incorrect. The 10% increase is applied to the new population that has already increased by 15%. The two consecutive increases of 15% and 10% are equivalent to a 26.5% single increase: $1.15 \times 1.10 = 1.265$.

Key Ideas

The Key Ideas summarize combining percents, calculating the increase in a number, and using percents of percents. As a class, discuss the methods to calculate the increase in a number. Students might suggest using 1.00 to represent the original cost of an item and adding the tax portion as decimals. Have students use examples to clarify the difference between combined percents and percents of percents. An example of combined percents might be adding two taxes such as PST and GST. An example of percents of percents might be discounting an item 10% off the original price and then discounting it a further 10% off the already reduced price. Have students prepare their own summary of the Key Ideas in the notes in their chapter Foldable. Suggest that they provide an example for each point in the Key Ideas.

Assessment	Supporting Learning							
Assessment as Learning								
Communicate the Ideas Have students complete #1 to #3. Use student responses to assess their understanding of combining percents and percents of percents. Encourage them to share their answer to #2 with a partner and listen to each other's explanation.	 Check each student's answers to the questions. These are key questions; make sure students understand the concepts before proceeding. Encourage students who need help with #1 to use base ten blocks or hundred grids to show their understanding. For #2, encourage students who prefer doing the calculations in more than one step to answer the question using the method of their choice. Encourage students who need help with their explanation for #3 to use a drawing or hundred grids and words to show the population of caribou after each year. 							



Check Your Understanding

Practise

Encourage students to use mental math strategies to solve problems involving percents. Note that #4 and #5, and #6 and #7, are pairs of similar questions. Consider assigning or allowing students to choose one question from each pair initially. You might assign the second question from each pair to those who would benefit from extra practice.

When doing #8, encourage students to estimate and then calculate the total tax and cost.

Apply

These questions provide a range of contexts for students to solve problems involving combined percents and percents of percents. You may need to remind students that all taxes are calculated separately.

Extend

These questions allow students to solve more complex problems involving percents. Encourage students to show more than one method.

Math Link

The Math Link provides an opportunity for students to solve problems involving percents.

11. A student is awarded a \$1000 scholarship

simple interest per year.

12. Simon Whitfield of Victoria,

British Columbia, won the men's triathlon at the Sydney Olympics. The race

consisted of a 1.5-km swim

in Sydney Harbour, a 40-km bike ride through Sydney

a) What percent of the race distance

b) What percent of the race distance

is each component? Express your

answer to the nearest tenth of a percent.

is spent on land? Express your answer to the nearest tenth of a percent.

13. A ski jacket has been marked down on three

occasions, first 20% off, then 25% off the

price. What is the overall percent saved?

14. The selling price of a DVD player is 35%

does the store still gain?

more than its cost. It is sold at a discoun of 20% off the selling price. How much

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new price, and finally 50% off the previous

and a 10-km run.

Extend

and places it in an account that pays 3%

a) What is the total value of the scholarship

amount at the end of the second year?

value of the scholarship after two years?

12 13 V.

b) What is the single percent increase in

Meeting Student Needs

- Some students may find it helpful to organize the information for #10 in a chart.
- Provide **BLM 4–12 Section 4.4 Extra Practice** to students who would benefit from more practice.

ELL

- Ensure students understand the terms *caribou*, *delayed*, *environment tax*, *scholarship*, *downtown core*, *ski jacket*, *faucet*, and *industry*.
- For #12, use the visual to help explain the three components of a triathlon (swimming, biking, and running).

Gifted and Enrichment

Number

of Trees

120 000

Year

- Allow students to use spreadsheet software and develop appropriate formulas to calculate tax.
- Challenge students to solve the following problem: A forest has 120 000 trees. Each year 20% of the trees are cut down, and 15 000 new trees are planted. How many trees are in the forest at the end of the fourth year? Have students use a table.

Number of

Trees Cut

Number

of Trees

Remaining

Number

of Trees

Planted

15000

Number

of Trees at

Year End

• For the Math Link, provide other examples of domestic uses of water, and have students calculate the percent of the water used daily that is wasted by a dripping faucet. Choose from uses such as the following: shower (5 min) uses 100 L; automatic dishwasher uses 40 L; dishwashing by hand uses 35 L; hand washing (with tap running) uses 8 L; brushing teeth with tap running) uses 10 L. Have students present their findings.

Common Errors

- Some students may try to add percent of percent values.
- R_x Model solving a percent of percent problem using a two-step process. Step 1 involves multiplying the item by the first percent. Step 2 involves multiplying the value of the item after the completion of step 1 by the second percent.

Answers

Math Link

a) approximately 13.9%

b) 0.027% or $\frac{27}{1000}$

Assessment	Supporting Learning
Assessment for Learning	
Practise Have students do #4 and #6. Students who have no problems with these questions can go on to #8 and the Apply questions.	 Provide additional coaching with Example 1 to students who need help with #4. Have them use the method they feel most comfortable with to solve the problem. Clarify any misunderstandings. Coach students through #4, and then have them complete #5 on their own. Check back with students several times to make sure that they understand the concepts. Provide additional coaching with Example 2 to students who need help with #6. Have them explain their thinking; clarify any misunderstandings. Consider coaching students through #6 by using a two-step process: multiply the item by the first percent, and then multiply the value of the item after step 1 by the second percent. Have students complete #7 on their own.
Math Link The Math Link on page 149 is intended to help students work toward the chapter problem wrap-up titled Wrap It Up! on page 153.	 It is recommended that all students complete the Math Link. Consider having concrete and kinesthetic learners measure the volume of water from a dripping tap over a set amount of time and then extrapolate how much that would be over a 24-hour period to give them a concrete understanding of the amount of water that is wasted. Students who need help getting started could use BLM 4–13 Section 4.4 Math Link, which provides scaffolding.
Assessment as Learning	
 Math Learning Log Have students describe a method they could use to determine the percent of water that is wasted in their household. To determine the percent of a number, you 	 Depending on students' learning style, have them provide oral or written answers. Encourage students to use the What I Need to Work On tab of their chapter Foldable to note what they continue to have difficulties with.