Rotation Symmetry and Transformations

MathLinks 9, pages 16–25 1.2 **Rotation Symmetry and** Suggested Timing **Transformations** 90–100 minutes Focus on... After this lesson, you will be able to... • tell if 2-D shapes and designs have rotation symmetry Some 2-D shapes and designs do not demonstrate line symme but are still identified as having strate line symmetry. **Materials** symmetry. The logo shown has this type of symmetry. What type of transformation can be demonstrated in this symbol? scissors give the order of rotation and angle of rotation for various shapes tracing paper isometric dot paper shapes create designs with rotation symmetry identify the transformations in shapes and designs involving line or • grid paper • ruler • paper clips (optional) rotation symmetry **Explore Symmetry of a Rotation** Materials **Blackline Masters** tracing paper Look carefully at the logo shown. Master 7 Isometric Dot Paper 1. The logo has symmetry of rotation. What do you think that means Master 8 Centimetre Grid Paper Copy the logo using tracing paper. Place your drawing on top of the original figure. Put the point of your pencil on the tracing paper and rotate the design until the traced design fits perfectly over the original design. BLM 1-4 Chapter 1 Warm-Up centre of rotation BLM 1–9 Section 1.2 Extra Practice the point about which the rotation of an object or design turns Original design. a) Where did you have to put your pencil so that you were able to rotate your copy so that if ft over the original? How did you decide where to put your pencil? Explain why it is appropriate that this point is called the <u>centre of rotation</u>. BLM 1–10 Section 1.2 Math Link rotation symmetry b) How many times will your tracing fit over the original design, in **Mathematical Processes** occurs when a shape design can be turned about its centre of rotation so that it fits one complete turn? Approximately how many degrees did you turn your tracing each time before it overlapped the original? Communication (C) ✓ Connections (CN) 3. Work with a partner to try #2 with some other logos or designs Mental Math and Estimation (ME) **Reflect and Check** 4. What information can you use to describe rotation symmetry Problem Solving (PS) ✓ Reasoning (R) MHR • Chapter 1 16 Technology (T) Visualization (V) Explore Symmetry of a Rotation **Specific Outcomes**

SS5 Demonstrate an understanding of line and rotation symmetry.

Category	Question Numbers
Essential (minimum questions to cover the outcomes)	#1–3, 4, 7, 9, 10, 12, 16, Math Link
Typical	#1–3, 4, 7, 9, 10, 12, 16, 17, 19, Math Link
Extension/Enrichment	#1-3, 10, 17-26, Math Link

Planning Notes

Have students complete the warm-up questions on **BLM 1–4 Chapter 1 Warm-Up** to reinforce material learned previously.

Have students examine the logo for Population Health. Discuss any symmetry demonstrated and relate the discussion to transformations.

Students may wish to use Master 7 Isometric Dot Paper and Master 8 Centimetre Grid Paper as they work through the section. In this Explore, students examine a logo for Population Health to determine characteristics of rotation symmetry. This activity should be completed individually since it is necessary for each student to physically rotate the design until it fits perfectly onto itself and then answer the questions in #2.

Students should find other logos or designs to explore in #2 from advertising brochures, magazines or newspapers, or the Internet.

Have students discuss #3 in pairs, then in larger groups, and then as a class. Challenge students to identify any aspect associated with a rotation in their response. As they discuss, ask:

- What do you need for a rotation to occur?
- How can you describe the turning associated with a rotation?
- What units can be used to measure the amount of rotation?
- If you need to check that a design has rotation symmetry, what is the first thing you should identify?

To help students better visualize rotation, have additional shapes prepared for students to examine.

Meeting Student Needs

• Students may benefit from working through the Explore as a whole-class activity.

ELL

- Teach the following terms in context: *tracing*, *turn*, *rotate*, and *original design*.
- Work through the steps with English language learners to ensure that they are able to follow them, or partner them with English-speaking students.

Gifted and Enrichment

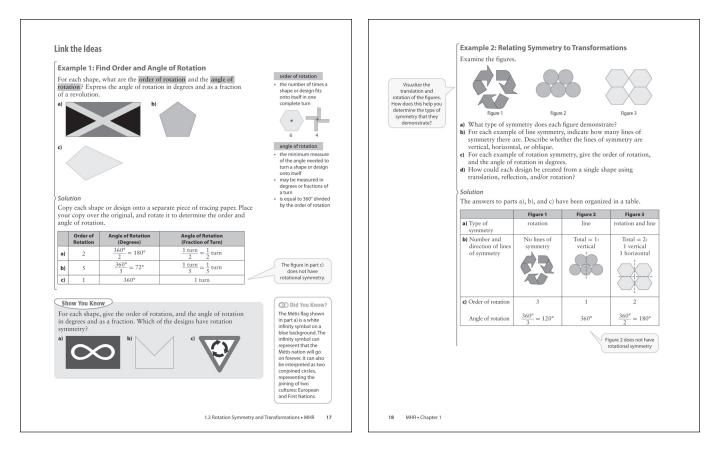
• Challenge students by having them investigate how to create flip cartoon books, and then have them create their own cartoon that uses rotation symmetry.

Answers

Explore Symmetry of a Rotation

- **1.** Symmetry of rotation means the symmetry of the image occurs when a part of the image is rotated onto itself.
- **2.** a) The centre of the rotation should be in the centre of the image.b) Three
 - **c)** 120°
- **4.** Example: Part of the image rotates to fit onto itself and the design is often circular.

Assessment	Supporting Learning
Assessment as Learning	
Reflect and Check Listen as students discuss what they discovered during the Explore. Try to have students generalize the information they use to describe <i>rotation symmetry</i> by encouraging statements that apply to all figures with rotation symmetry.	 Encourage students to write their description in their Foldable. Have them share their explanation with a partner. Encourage students to share their ideas for #4. In a large group discussion, have students decide what always could be used to describe <i>rotation symmetry</i> in a given figure, Have students give examples or non-examples to support their position.



Link the Ideas

Example 1

Have students try Example 1, based on their prior knowledge. For each figure in Example 1, ask students to describe the location of the centre of rotation they are using. You may wish to ask questions such as:

- Can the centre of rotation be outside the figure?
- Does the number of sides in a figure affect the angle of rotation?

Have all students complete the Show You Know to ensure that they understand the concept of rotation symmetry and its associated terminology. Draw students' attention to the Did You Know? about the Métis flag.

Example 2

It might work well to complete Example 2, using one of the given figures with the entire class, and then have students attempt the questions with the two remaining figures, either individually or in pairs. Some students may be confused with part d). Explain that each figure is made by repeating a part of itself. Ask:

- What shape is repeated for each figure?
- How many times has the shape been repeated in each figure?

- Which figure could be created using only translations? How many?
- Which figures can be created using reflections?
- Which figures can be created using more than one transformation?

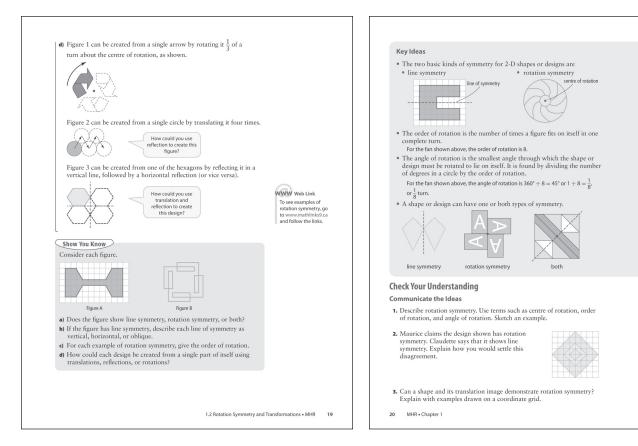
Have students work on the Show You Know individually or with a partner. Encourage each to explain their answer to part a) orally in order to see if mathematical vocabulary is correctly used.

Key Ideas

The Key Ideas provide a summary of the main ideas from section 1.2, with different examples from those shown previously. Students should not copy these Key Ideas as notes but rather make their own notes by identifying vocabulary, concepts, and methodology that are important to them. Have students record their ideas in their Foldable or notebook.

Meeting Student Needs

• To help students with their organization skills, remind them that a chart can be a good way to present part or all of the solution for a mathematical problem. Discuss with students why the charts in Example 1 and 2 seem to work.



- Some students benefit from physically rotating their own body using a 90° or a $\frac{1}{4}$ turn rotation. Have other students describe the view after each 90° rotation.
- Students may benefit from working through the examples as a whole-class activity.
- Remind students that the term *rotation* means to turn around. Inform students that one full turn is 360° , a half a turn is $360^{\circ} \div 2 = 180^{\circ}$, and a quarter turn is $360^{\circ} \div 4 = 90^{\circ}$.
- To help students determine the order of rotations, have them trace the figure and then cut it out. Place the cut-out figure on top of the original and have the students turn it. Each time the cut-out figure matches the original is one order of rotation.
- Some students may benefit from rotating their figure about a vertex point until they become comfortable with the rotations. They can move to point symmetry by drawing a line from a vertex to the point of symmetry. Watching the line as the figure is rotated may be somewhat easier for students to visualize.
- Students may benefit from working through the Show You Know questions with a partner or in small groups.

ELL

• Teach the following terms in context: *fraction of a revolution* and *rotation symmetry*.

Common Errors

- Some students may have difficulty identifying the single shape from which a figure is created or describing the transformations needed to make it.
- R_x In Example 2, begin with Figure 3, then Figure 2, and finally use Figure 1. Figures 2 and 3 are relatively easy for students to create using translations. Figure 1 requires rotations.

Answers

Example 1: Show You Know

a) Order of rotation = 2, angle of rotation = 180°b) No rotation symmetry

c) Order of rotation = 3, angle of rotation = 120°

Example 2: Show You Know

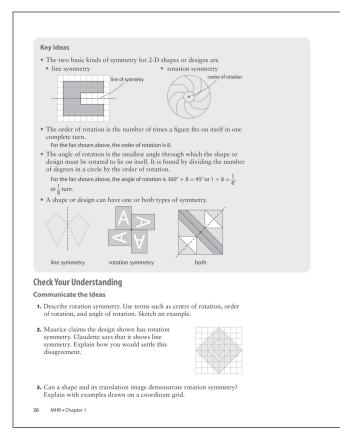
a) A: both; B: rotation symmetry

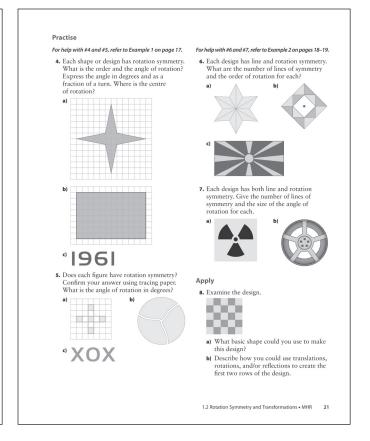
b) A: vertical line and horizontal line

d) A: reflection about a vertical or a horizontal line; B: rotation about the centre

Assessment	Supporting Learning			
Assessment for Learning				
Example 1 Have students do the Show You Know related to Example 1.	 Encourage students to verbalize their thinking. You may wish to have students work with a partner. Give students a similar problem to solve. Allow time for students to work with a partner and to talk through their thinking in arriving at the solution. For variation and to extend understanding, give students the angle of rotation and ask them for the order of rotation and for an example that satisfies the conditions. 			
Example 2 Have students do the Show You Know related to Example 2.	 Encourage students to verbalize their thinking. You may wish to have students work with a partner. Some students may benefit from copying the shapes and being able to manipulate them to answer parts a) and b). For part c), remind students that the term <i>rotation</i> means to turn around. Inform students that one full turn is 360°, a half turn is 360° ÷ 2 = 180°, and a quarter turn is 360° ÷ 4 = 90°. Part d) requires students to combine the concepts in the lesson and use previous skills to identify ways of generating the shapes. Students experiencing difficulty will benefit from a hands-on approach. For Figure B, consider giving students paper clips and allowing them to rearrange them to answer the question. If students are not having difficulty, you may wish to introduce a tessellation and ask students to identify the repeating shape and the transformations used to create the pattern. Have students explain, using models or diagrams, the connection between rotation symmetry and transformations. Emphasize that many examples of rotation symmetry have more than one combination of transformations that can be used to generate the figures or design. 			

c) A: 2; B: 4





Check Your Understanding

Communicate the Ideas

Have students work individually or in pairs to answer the assigned questions. In #1, students are asked to describe rotation symmetry using an example. Their description gives them the opportunity to use mathematical terminology.

In #2, students are asked to settle a disagreement between two students. One claims that a figure has rotation symmetry, while the other says it has line symmetry. It turns out that they are both correct.

Students may find #3 more difficult as it is an extension-type question. Students are asked to indicate if a shape and its translation image can demonstrate rotation symmetry. The answer depends on the initial shape. If the shape is a square, it is possible to translate it over and down to create what looks like rotation symmetry. For most shapes, it is not possible to translate the shape and end with rotation symmetry.

Practise

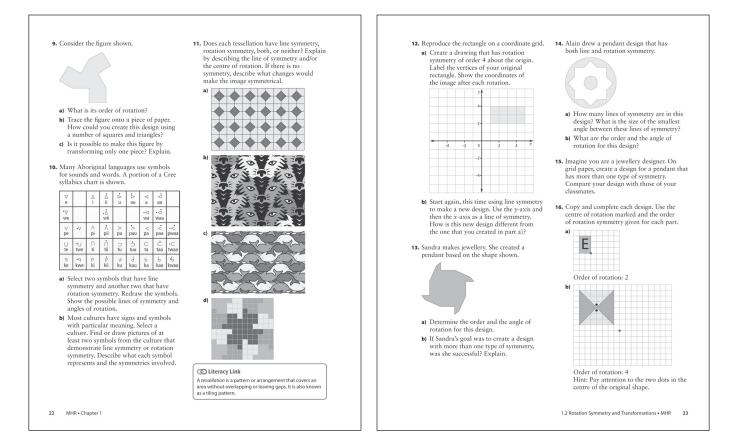
Students could be given a choice of one question within each of the pairs of questions (#4 or 5, #6 or 7) since each pair is similar.

Students should work individually on these questions and then check against the answers in the back of the student resource.

Apply

Note that #8, 9, 11, 14, and 16 relate rotation symmetry to designs and emphasize the mathematical aspects of the symmetry, often in relation to transformations. When students work on #11, you may wish to have them research Cree symbols. Refer to the related Web Link that follows.

Note that #10, 13, 15, and 17, 19, 20 to 23 are rooted in applications of rotation symmetry in the world around us. These questions introduce students to the usefulness of rotation symmetry in our lives.



Extend

In #26, students are asked a theoretical question relating to the rotation of a chord of length r, where r is the radius of the circle. Students should be encouraged either to draw the situation, model it using toothpicks, or model it on Geometer's Sketchpad. Question #24 relates rotation symmetry to the number of teeth on gears and vice versa.

Literacy Link At the end of section 1.2, have students complete the left circle of the thematic map. Brainstorm and discuss as a class the information needed to complete the rectangle boxes and accompanying definitions.

Math Link

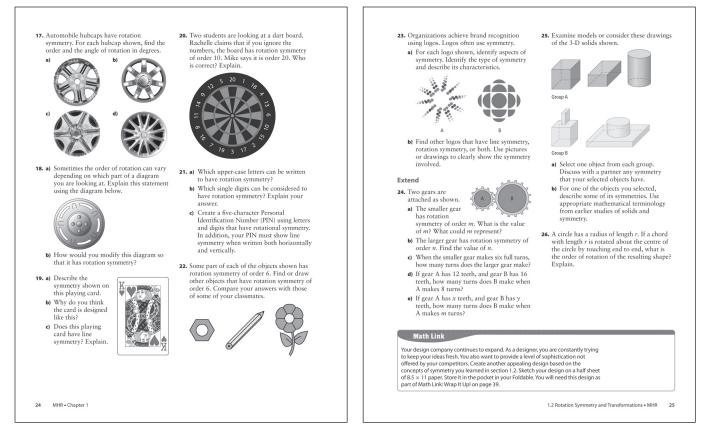
This Math Link continues the theme introduced in section 1.1. Students are designers trying to come up with fresh, new design ideas. This time, they must limit their designs to rotation symmetry and the ideas used in section 1.2. The design created here is to be stored and used as part of the Math Link: Wrap It Up! at the end of the chapter.

WWW Web Link

To find out more about Cree Syllabics, go to www.mathlinks9.ca and follow the links.

Meeting Student Needs

- Provide **BLM 1–9 Section 1.2 Extra Practice** to students who would benefit from more practice.
- Give students as much variety and choice as possible to encourage them to take responsibility for their learning. Variety can provide differentiated learning opportunities.
- All students should attempt the Math Link as it is a non-threatening, fun way to explore symmetry as they create a design.



ELL

- Teach the following words in context: *sketch*, *claims*, *settle* (a disagreement), *disagreement*, *coordinate grid*, *fraction of a turn*, *gears*, *teeth* (on a gear), *sophistication*, and *competitors*.
- Students may find some of the more language-dense questions to be a challenge. Reduce the number of questions assigned, and ensure that students understand the questions they are being asked.

Common Errors

- Some students may not see rotation symmetry in drawings and pictures.
- R_x Ensure that students can quickly identify the centre of rotation. This is normally in the centre of the shape or object. Once the centre is located, encourage students to trace the shape on a separate piece of paper, cut it out, and physically rotate it about the centre of rotation. Remind students that this approach to visualizing the rotation can help them solve every problem on rotation symmetry.

Answers

Communicate the Ideas

1. Rotation symmetry occurs when a section of a design can be rotated about a centre point and shows symmetry with other parts. Example:



- **2.** Both Claudette and Maurice are correct. The design shows both line and rotation symmetry. The design can be folded over a horizontal or vertical line of symmetry to overlap itself, or a corner piece can be rotated four times to create the design.
- **3.** Yes. Any regular object (for example, a square or hexagon) with equal side-lengths can be translated horizontally or vertically and still maintain rotation symmetry with the original. Example:

				y,	1		
-	_	_	_				>
*							x
•							×
•							x

Assessment	Supporting Learning
Assessment as Learning	
Communicate the Ideas Have all students complete #1–3.	 Encourage students to verbalize their thinking. You may wish to have students work with a partner. For #1, if students have difficulty, encourage them to select an example of rotation symmetry from Example 1 or 2. Have students brainstorm possible terms that could be used to describe rotation symmetry in #1. Have a class discussion about the possible responses to #2. This question links directly to #3. Have students work in pairs to complete #3. They should be encouraged to demonstrate their shape and their explanations to the class. For students experiencing difficulty with #3, provide them with a shape that will meet the criteria and change the question to "Explain and show how this shape and its translation demonstrate rotation symmetry." You may wish to have students assess each other's responses, using Master 2 Communication Peer Evaluation.
Assessment for Learning	
Practise and Apply Have students do #4, 7, 9, 10, 12, and 16. Students who have no problems with these questions can go on to the remaining Apply questions.	 If students have difficulty with #4 or 7, provide additional coaching using Example 1 and Example 2, respectively. Then, have them do #5 and 6 on their own. Note that students will require tracing paper to complete the check in #5. In #10, a portion of a Cree Syllabics chart is used. It is useful to point out that symmetry has been part of language throughout history. This question provides an opportunity for students to see symmetry in the Cree culture. Remind students that they are choosing the symbol and not the word below it. For students who get overwhelmed by choice, limit their search to the first two rows or a limited number of boxes. In #12, students have the opportunity to use coordinate geometry to track reflections and rotations. Provide students with a large enough grid for them to manipulate their shape. For students who are having difficulty with #16, provide a grid and the shape that they can cut out. For the visual leaner, it might be easier if the grid was 1-cm grid paper.
Math Link The Math Link on page 25 is intended to help students work toward the chapter problem wrap-up titled Math Link: Wrap It Up! on page 39.	 Students who need help getting started could use BLM 1–10 Section 1.2 Math Link, which provides scaffolding. Have students go back to their original design for the section 1.1 Math Link and see if their original design already has symmetry in it that they could expand upon. Reinforce that the Math Link is a necessary part of the Math Link: Wrap It Up! on page 39. Have students show their progress after a set amount of time. This will motivate students to get started and feedback may give them some ideas. Emphasize the creative aspects of this assignment and discourage students from picking up ideas from others.
Assessment <i>as</i> Learning	
Literacy Link (page 3) Help students to recall the new terms introduced in this section by adding them to their map.	• Have students complete the left circle by adding the following terms: <i>order</i> , <i>angle</i> , and <i>centre of rotation</i> . Have students write their own definitions and create an example for each term.
 Math Learning Log Have students respond to the following prompts: The mathematical vocabulary I can use to describe rotation symmetry is The similarities and differences between line symmetry and rotation symmetry are 	 Encourage students to use the What I Need to Work On section of their Foldable to note what they continue to have difficulties with. Have students present answers in oral, written, poster, or PowerPoint format. Encourage students to use specific examples in their presentations.