Enlargements and Reductions

MathLinks 9, pages 130–138

Suggested Timing

80-100 minutes

Materials

- tracing paper
- ruler
- grid paper
- computer with Internet access (optional)

Blackline Masters

Master 2 Communication Peer Evaluation Master 8 Centimetre Grid Paper Master 9 0.5 Centimetre Grid Paper Master 10 2 Centimetre Grid Paper BLM 4–3 Chapter 4 Warm-Up BLM 4–5 Section 4.1 Extra Practice BLM 4–6 Section 4.1 Math Link

Mathematical Processes

- Communication (C)
- Connections (CN)
- Mental Math and Estimation (ME)
- Problem Solving (PS)
- 🖌 Reasoning (R)
- Technology (T)
- Visualization (V)

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Specific Outcomes

SS4 Draw and interpret scale diagrams of 2-D shapes.

Category	Question Numbers
Essential (minimum questions to cover the outcomes)	#1, 2, 4a) <i>or</i> b), 6a) <i>or</i> b), 7, 9, Math Link
Typical	#1, 2, 4a) <i>or</i> b), 6a) <i>or</i> b), 7, 9, 11, 13, Math Link
Extension/Enrichment	#1, 2, 13, 15, 16 or 14 and 17, Math Link

Planning Notes

Have students complete the warm-up questions on **BLM 4–3 Chapter 4 Warm-Up** to reinforce material learned in previous sections.

In this section, students identify and draw enlargements and reductions to scale and interpret the scale factor.



4

As a class, discuss the opening questions about using a microscope. Use students' ideas to gauge what students recall about magnification from earlier science courses. Direct them to the information about how to calculate total magnification. Discuss the Did You Know? about the magnification power of microscopes in the science lab. Depending on what your students recall, you may need to discuss terms so they are able to complete the Explore. Consider collaborating with a science teacher to demonstrate using a microscope to help make the connections for students.

Explore How to Enlarge an Image

In the Explore, students investigate ways to make an enlargement. Before they begin, direct students to the margin definition for *enlargement* on page 131 in the student resource, and clarify that *constant factor* refers to multiplying each dimension by the same amount. Explain that each dimension of the enlarged smiley face is twice the length of the corresponding length of the original. Invite students to verify this using a ruler to measure the diameter and/or the radius.



Method 1 Have students work with a partner to discuss #1. Encourage students to try any strategies that they can think of to make the enlargement. Have students work individually to complete #2. Make tracing paper and **Master 8 Centimetre Grid Paper** available. Circulate as students work and ask them to verify if their enlargement meets the ratio requirements. Prompt them to recall that a ratio of 2:1 means that each dimension of the enlargement is two times the length of the original.

For #3, have students compare their diagram(s) with their partner's, and then discuss their strategies and the advantages and disadvantages of each strategy with another pair of students before presenting their findings to the class. Have students work with their partner to discuss #4 before writing an individual response. As they work, circulate and prompt students to use math vocabulary when explaining their method.

Method 2 As a class, have students brainstorm strategies and then work in small groups to try out at least one of the strategies. Have groups present their strategies to the class and discuss their advantages and disadvantages.

Meeting Student Needs

- It may benefit concrete and kinesthetic learners to use a microscope and view an onion slide. You might use the eyepiece and the objective lens to point out the magnification on each, and then calculate the total magnification.
- For the images of the smiley face in the margin definition for enlargement, you might explain that although each 1-D measurement on the enlarged image is twice as large, the area is four times as large. You might invite students to find out if this is true.
- For the Explore, you might use a cell with more visible organelles for students who are interested. A paramecium and a planarian have simple shapes with easily reproducible details.
- Consider working through the Explore as a whole class.

ELL

- Some students may find it useful to remember that the term *enlargement* contains the word *large*. This may help them to remember that an enlargement is larger than the original.
- Some students may not be familiar with terms such as *magnifies*, *naked eye*, *enlarged*, *onion skin*, *magnification*, *eyepiece*, *objective lens*, *onion cell*, and *twice as large*. Explain each term in context and have students add any new terms to their personal dictionary.

Gifted and Enrichment

• Challenge students to find out how binoculars work and how the images seen relate to what they are learning about enlargements.

Answers

Explore How to Enlarge an Image

- **1.** Examples:
 - Multiply the length and width of the cell by the same number.
 Use an overhead projector to enlarge the image.
- **4.** a) Example: Measure the length and the width of the image and divide each measurement by 2. The answers should correspond to the length and the width of the original.

- The enlargement and the original have the same proportions for length and width.
- Difference:
- The measurements of the lengths and widths are different.

b) Example:

Similarity:

Assessment	Supporting Learning
Assessment as Learning	
Reflect and Check Listen as students discuss what they discovered during the Explore.	 Some students may benefit from the class discussion as a springboard to develop their own response. For #4a), record the methods on the board. Encourage students to include a summary of the methods in their Foldable. Consider having students verbalize their method to a classmate before recording it. For #4b), remind students to refer to the original and enlarged images of onion cells to make the comparison.





Link the Ideas

Example 1

Example 1 illustrates two methods for drawing an enlargement, namely, using grid paper and using a scale factor. Students may have discussed both of these methods during the Explore. If so, guide students to use these two methods and draw the picture shown in the student resource. If using a scale factor was not a strategy discussed during the Explore, walk through the method as a class.

Before students use grid paper to enlarge the picture, you may wish to use a simple shape such as a rectangle superimposed on centimetre grid paper and demonstrate how to copy the contents of each grid square onto the corresponding square of 2-cm grid paper. Make Master 8 Centimetre Grid Paper and Master 10 2 Centimetre Grid Paper available to students. As they work, circulate and check that students are drawing the contents of squares correctly.

You might introduce Method 2 by asking students how they would draw an enlargement if grid paper was not available (measure line segments). Have students measure to check the length of the line segments. Discuss the definition for *scale factor* and then ask them to draw the rectangle that contains both arrows, twice as large. Ask them to identify the scale factor of the enlarged rectangle (2). Then, guide them to use the measurements of the original and enlarged rectangles to determine the position of the arrows and the measurement of the arrows in the enlarged rectangle.



Have students work individually on the Show You Know, and then exchange their enlargement with that of a classmate. Have them verify whether the image is an accurate enlargement by checking whether each dimension is three times larger.

Example 2

Example 2 illustrates two methods for drawing a reduction, namely, using grid paper and using a scale factor. Before beginning, discuss the definition for *reduction* and ask students for applications of reductions that they are familiar with.

Similar to the process for Example 1, guide students to work through the example. Make **Master 8 Centimetre Grid Paper** and **Master 9 0.5 Centimetre Grid Paper** available.

For Method 2, mention that multiplying by 0.5 or $\frac{1}{2}$ is the same as multiplying by 2.

Discuss the thought bubble that describes using the scale factor to determine if an object is a reduction or an enlargement.

As a class, have students discuss the method they prefer for making reductions and explain why.

Have students work individually on the Show You Know, and then exchange their reduction with a classmate's. Have them check whether the image is an accurate reduction by checking that each dimension is half as large.

Key Ideas

The Key Ideas define enlargements and reductions and how to draw them, as well as scale factors and how to interpret them. Have students use their Foldable to make their own summary of the key ideas about enlargements and reductions, and provide their own example of using grid paper and a scale factor to enlarge and reduce an image to scale.

Meeting Student Needs

- Consider working through Examples 1 and 2 as a whole class and having students work in pairs to complete the Show You Knows.
- For Method 1 in both examples, some students may find it helpful to use a copy of the picture already superimposed on grid paper, so they do not have to trace it.



- Some students may benefit from using a map grid by numbering each square on the grid of the original and each corresponding square on the grid of the image. Point out the example of the map grid on page 131 in the student resource. You might have students note how a map grid is different from a coordinate grid. (A coordinate grid names the intersections of grid lines.)
- For Example 1, instead of using 1-cm and 2-cm grid paper, consider having students use 1-cm grid paper for the entire activity, For example, if a line

segment on the original is 2 cm in length, draw a line segment 4 cm in length on the image.

- For Example 2, consider having students trace the original on 2-cm grid paper, and then draw the contents on 1-cm grid paper.
- Some students may benefit from completing an additional Show You Know related to each example. For Example 1, have students draw an enlargement of a hexagon on a 1-cm grid using a scale factor of 4. For Example 2, have students draw a reduction of a hexagon on a 2-cm grid using a scale factor of 0.25.

ELL

• Teach the following words in context: *grid lines, constant, half as large,* and *line segment.*

Common Errors

- Some students may not enlarge or reduce all dimensions of the original picture when drawing the image.
- R_x Clarify that each dimension must be enlarged or reduced using the same scale factor.

Answers

Example 1: Show You Know

Look for a drawing for each of two methods. Example:

- Multiplying each measurement by a scale factor of 3, and using the new lengths to draw the enlargement.
- Using 1-cm grid paper and drawing the contents of each square in 3 squares.

Example 2: Show You Know

Look for a drawing using a method that students choose. Example: Drawing the contents of each square on 0.5-cm grid paper

Assessment	Supporting Learning
Assessment for Learning	
Example 1 Have students do the Show You Know related to Example 1.	 Encourage students to verbalize their thinking. You may wish to have students work with a partner. Some students may benefit from using a ruler. Encourage students to start with the method they are most comfortable with. Have them compare methods with a partner. List the methods on the board.
Example 2 Have students do the Show You Know related to Example 2.	 Encourage students to verbalize their thinking. You may wish to have students work with a partner. Some students may benefit from using a ruler. Encourage students to start with the method they are most comfortable with. Have them compare methods with a partner. List the methods on the board. Have students discuss and make notes about what a scale factor of 1, less than 1, or greater than 1 means.



Check Your Understanding

Communicate the Ideas

These questions provide an opportunity for students to explain their understanding of enlargements, reductions, and interpreting the scale factor. Have students provide an individual response to all questions.

Have students work individually to answer #1 and 2, and then discuss their reasoning with a partner or small group.

For #1, students explain their understanding of reductions. Encourage students to use math vocabulary.

For #2, students identify an error in using a scale factor to make an enlargement. Encourage students to draw the enlargement to check the answer.

For #3, students describe two methods for making an enlargement. Encourage students to use diagrams in their response. They may find it easier to trace the logo on grid paper. Some students may benefit from describing both methods to a partner before writing their response.

Practise

Note that #4 and 5 and #6 and 8 are sets of similar questions. Consider giving students a choice to do one question from each set initially to demonstrate their understanding.

Make Master 8 Centimetre Grid Paper, Master 9 0.5 Centimetre Grid Paper, and Master 10 2 Centimetre Grid Paper available to students.

Encourage students to use the method of their choice to draw enlargements or reductions.

For #7, have students explain their reasoning to a classmate.

Apply

These questions allow students to apply their understanding of enlargements, reductions, and scale factors in a variety of contexts.

Use #9 and 11 to assess understanding of enlargements and reductions, and scale factors.

For #10, direct students to the Did You Know? that describes the Festival du Voyageur. You might explain that *joie de vivre* means joy of living.

For #13, make grid paper available to students.



Extend

The questions in this section allow students to make connections to real-life applications.

Make grid paper available to students.

For #15, students will need more than one sheet of 8.5×11 paper. Consider giving students an option to use a pattern in a craft magazine. Have them enlarge or reduce the pattern given to actual dimensions.

Since #14, 16, and 17 are similar questions, you might allow students to choose one of these questions; alternatively, you might assign one.

For #16, you might limit the number of items students need to include in the scale diagram.

For #17, students need to use percent to reduce the original lengths of line segments.

Literacy Link Direct students to the leg on their spider map entitled Enlargements and Reductions and have them complete definitions for *enlargement*, *scale factor*, and *reduction*, using words, diagrams, and mathematical expressions. Encourage them to include an example for each term.

Math Link

The Math Link allows students to apply their understanding of drawing enlargements and reductions to scale. It is important for all students to complete each Math Link throughout the chapter in order to complete the Wrap It Up! at the end of the chapter.

In this Math Link, students choose a project that requires a scale diagram, research their project using the library or the Internet, and use grid paper to draw a scale diagram. Although a list of design projects is provided, encourage students to choose a topic of personal interest, such as decorating a wall using mosaic patterns, and then get your approval before proceeding. Emphasize to students that they will build on their project design throughout the chapter.

Provide students with access to the library and/or the Internet to help them select a design project, and make grid paper available for them to draw their design to scale.

Meeting Student Needs

- For #12, encourage students to draw the flag on grid paper.
- Provide **BLM 4–5 Section 4.1 Extra Practice** to students who would benefit from more practice.

ELL

- For #1 to 3, allow English language learners to discuss their ideas in their first language, and then develop their response in English. This offers them the opportunity to activate their knowledge using familiar language. Afterwards, it may be easier for them to ask for the missing vocabulary to express their thinking in English.
- For #7, explain that *indicate* means state.
- For #11, clarify that a *true reduction* means that Figure B is an accurate reduction of Figure A. In other words, each dimension of Figure B has been reduced by the same scale factor.
- For #13 and 15, explain that a pattern is a paper template of each part of an item, such as a laptop bag. The pattern pieces are traced onto fabric before cutting out and assembling the item.
- Ensure students understand the following terms: human cheek cells, French Quarter, fur traders, Red River colony, Heritage Fair, hunting dress, hopscotch, recreational area, outfit, fashion show, automotive course, landmark tourism, and contemporary drum designs. Have students add any new terms to their dictionary.

Gifted and Enrichment

- Challenge students to draw a reduction of a structure they are familiar with. For example, they might research the actual dimensions of a tipi and then use a scale factor to draw a scale diagram.
- Invite students to explore enlargements and reductions using a scale factor by accessing the Web Link described in the student resource on page 136.

Answers

Communicate the Ideas

- **1.** Example: Yes, the photos are reduced from the original in order to fit on the page, but they retain the same proportions as the original.
- **2.** Example: No, she is correct only for the enlargement of the side length that measures 3 cm. The enlargement for the 5-cm side length should be 15 cm.
- **3.** Examples:
 - Use grid paper. Superimpose the logo on 0.5-cm grid paper. Then, draw the contents of each grid square into the corresponding region on larger-size grid paper. The area of the grid paper should match the space for the logo on the poster.
 - Use a scale factor. Measure the length and width of the logo. Measure the length and the width of the space for the logo on the poster. Determine the scale factor needed for the enlargement. Then, use the scale factor to enlarge each dimension of the logo.

Assessment	Supporting Learning	
Assessment <i>as</i> Learning		
Communicate the Ideas Have all students complete #1 and 2.	 Encourage students to verbalize their thinking. You may wish to have students work with a partner. Students may benefit from drawing the rectangle in #2, and then enlarging it using a scale factor of 3 to check their answer. You may wish to have students use Master 2 Communication Peer Evaluation to assess each other's responses to #1 and 2. 	
Assessment <i>for</i> Learning		
Practise and Apply Have students do #4a) <i>or</i> b), 6a) <i>or</i> b), 7, and 9. Students who have no problems with these questions can go on to the remaining Apply questions.	 Students who need assistance with #4 may benefit from additional coaching with Example 1. Have them use a ruler and work through #4a) together. Then, have them try #4b) on their own to check for understanding. Students who need assistance with #6 may benefit from additional coaching with Example 2. Coach students through #6a). Then, have them try #6b) on their own. For #7, provide coaching to students who need it. You might use an overhead and apply a scale factor of 1, less than 1, and greater than 1 to an image. For each image, have students identify whether it is an enlargement, reduction, or neither, and then make a connection to the scale factor used to create the image. For #9, have students verbalize the meaning of <i>scale factor</i>. You might ask students to calculate the magnification for different objective lenses in a microscope. Prompt students to observe that as the magnification increases (scale factor increases), the image is enlarged. 	
Math Link The Math Link on page 138 is intended to help students work toward the chapter problem wrap-up titled Wrap It Up! on page 163.	 It is recommended that all students complete the Math Link. Some students may benefit from being directed to web sites or library resources to gather ideas for their design project. Some students may benefit from being provided with a start to the design of their choice. Encourage students to make revised sketches of their design if they make revisions to the initial design. Students who need help getting started could use BLM 4–6 Section 4.1 Math Link, which provides scaffolding. 	
Assessment <i>as</i> Learning		
Literacy Link By the end of section 4.1, have students complete definitions for <i>enlargement</i> , <i>scale factor</i> , and <i>reduction</i> .	 Some students may benefit from using their Foldable to record definitions for terms as they are introduced. Then, at the end of the section or the chapter, have them summarize the definitions in their own words and organize them on the spider map. For the examples students include on their spider map, encourage them to use scale factors that are natural numbers to describe enlargements and reductions. This may help them to understand, for example, that a scale factor of 2 means the image is twice as large as the original. Some students may find it helpful if you show them an actual enlargement and a reduction, and then have them describe each orally before writing a definition. Clarify any misunderstandings. 	
 Math Learning Log Have students respond to the following questions: How can you determine the scale factor used in an enlargement or a reduction? How can you use the scale factor to draw an enlargement? How can you use grid paper to draw a reduction? 	 Encourage students to refer to their notes in their Foldable or spider map. Encourage students to reference an example of an enlargement or reduction to help explain how to determine the scale factor. Encourage students to use diagrams to help with their explanations. Depending on students' learning styles, have them provide oral or written answers. Encourage students to use the What I Need to Work On section of their Foldable to note what they continue to have difficulties with. 	