

12110

### **Place Value**

Get Ready

| Arranging numbers in place value charts can help with estimation.<br>The place value chart below shows 1247.63. |   |      |      |                      |        |             |   |  |
|---|---|------|------|----------------------|--------|-------------|---|--|
| Thousands   | Hundreds  | Tens | Ones | <b>Decimal Point</b> | Tenths | Thousandths | ] |  |
| 1   | 2   | 4    | 7    | •                    | 6      | 3           |   |  |
| The numbe<br>The numbe<br>The numbe   | 1       2       4       7       •       6       3         The number 1248.63 is one more than 1247.63.         Look at the ones place. 7 + 1 = 8         The number 1147.63 is one hundred less than 1247.63.         Look at the hundreds place. 2 - 1 = 1         The number 1247.83 is two tenths more than 1247.63.         Look at the tenths place. 6 + 2 = 8 |      |      |                      |        |             |   |  |

**1.** Arrange the numbers in the place value chart.

|                   | Thousands | Hundreds | Tens | Ones | Decimal<br>Point | Tenths | Hundredths | Thousandths |
|-------------------|-----------|----------|------|------|------------------|--------|------------|-------------|
| <b>a)</b> 1349.52 |           |          |      |      |                  |        |            |             |
| <b>b)</b> 45.069  |           |          |      |      |                  |        |            |             |
| <b>c)</b> 100.05  |           |          |      |      |                  |        |            |             |
| <b>d)</b> 0.455   |           |          |      |      |                  |        |            |             |

### **Compare and Order Numbers**

You can use a place value chart to compare and order numbers. The numbers 270, 2.7, and 27 are shown in the following place value chart.

|     | Hundreds | Tens | Ones |   | Tenths |
|-----|----------|------|------|---|--------|
| 270 | 2        | 7    | 0    | • | 0      |
| 2.7 | 0        | 0    | 2    | • | 7      |
| 27  | 0        | 2    | 7    | • | 0      |

The numbers arranged from greatest to least are 270, 27, and 2.7. You can write this as 270 > 27 > 2.7.

- 2. Arrange each set of numbers from greatest to least.
- **3.** Use the symbol > to show the numbers arranged from greatest to least.

**a)** 1.9, 2.4, 2 **b)** 5, 4.3, 0.7

The symbol > means

"is greater than."

a) 1.8, 2.8, 1.9

**b)** 365.7,358, 365.9

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### **Use Mental Mathematics**

Mental mathematics includes estimating and calculating answers mentally. When asked to estimate, give an approximate but carefully thought-out answer. To mentally calculate, look for numbers that are easy to work with. To estimate  $2530 \div 7$ , work with numbers that are easy to calculate mentally. Low estimate.  $\circ \circ \circ \circ \circ$  $2100 \div 7 = 300$ 7 divides evenly into  $2800 \div 7 = 400$ High estimate. both 2100 and 2800. The answer to  $2530 \div 7$  is between 300 and 400. To mentally calculate 98 + 59, look for numbers that are easy to work with. Add 2 to 98 to make 100. 98 + 59 = 100 + 570000 Subtract that 2 from 59. = 157 59 - 2 = 57.

4. Calculate each answer mentally. Show your thinking.

a) 97 + 49

**b**) 99 × 5

Date:

### **Order of Operations With Whole Numbers**

Mathematicians use a set order of operations when calculating number expressions. Step 1: Do operations in brackets. () **Step 2:** Multiply and divide in order from left to right.  $\times, \div$ **Step 3:** Add and subtract in order from left to right. +, - $5 \times 5 + 20 \div (5 - 3) - 3 \times 2$ Brackets.  $= 5 \times 5 + 20 \div 2 - 3 \times 2$ Multiply and divide in order. = 25 + 10 - 6Add and subtract in order. = 35 - 6 = 29

<sup>₽</sup>E

- **5.** Calculate  $83 \times 7 + 234 \div 6$ . Show your steps.
- **7.** Calculate the value of each expression.
  - a)  $(21 12) \times 9 + 8$
- **6.** Evaluate without using a calculator.

a)  $14 + 3 \times 8 + 5 \times 6$ 

**b)**  $3 \times 5 + 16 \div 4 - 12 \div 3$ 

**b)**  $(34 - 6) \div 7 \times 3$ 

# 2.1 Add and Subtract Decimal Numbers

MathLinks 7, pages 48-55

## **Key Ideas Review**

Write the word or number from column B that matches each description in column A.

| Α  | В   |
|--|---|
| 1. One tenth   | a) Estimate   |
| 2. An estimate that is smaller than the actual answer      | <b>b)</b> Overestimate                              |
|  | c) Underestimate                                    |
| 3. Can be a place holder                                   | d) Front-end  |
| 4. Ten hundredths  | estimation  |
| 5. An estimate that is larger than the actual answer       | <ul> <li>e) Relative size<br/>estimation</li> </ul> |
|  | <b>f)</b> 0   |
| 6. An estimate in which only the leading digit stays       | <b>g)</b> 0.1                                       |
| 7. An estimate in which the leading digit may be increased | <b>h)</b> 0.10                                      |
| by one   | i) 0.100  |

## **Practise and Apply**

8. Without calculating the answer, c) 15.22 + 7.06 + 0.45 = 2273place the decimal point in the \_\_\_\_\_ + \_\_\_\_\_ + \_\_\_\_ = correct position. Show the estimate that helped you place the decimal d) 156.08 + 522 + 909.5 = 158758point. \_\_\_\_\_+ \_\_\_\_\_ = a) 35.27 + 61.84 = 9711\_\_\_\_\_ + \_\_\_\_\_ = \_\_\_\_\_ e) 782.56 - 258.76 = 5238 **b)** 81 + 14.074 + 201.897 = 296971\_\_\_\_\_ = \_\_\_\_\_ \_\_\_\_\_ + \_\_\_\_\_ + \_\_\_\_\_ = f) 268.7 cm - 58.22 cm = 21048 cm \_\_\_\_\_ = \_\_\_\_\_

#### Name:

9. Calculate.

| a) | 75.2<br>+ 6.5                    | b)      | 68.54<br>6.43<br>+ 55.08 |
|----|----------------------------------|---------|--------------------------|
| c) | \$513.69<br>\$49.06<br>+ \$40.00 | d)      | \$912.99<br>\$618.00     |
| e) | 92.00 m<br>– 8.76 m              | ,<br>f) | 5.612 cm<br>– 1.008 cm   |

- Date: \_\_\_\_
- 11. Ryan says that 1.5 + 2.20 = 1.05 + 2.20, since 0 is always a placeholder. Do you agree? Explain.
- **12.** The perimeter of the pentagon is 63.1 cm. What is the length of the side without a measurement label?



- **10.** Put the correct number in the box to make each of the following statements true. Show your thinking.
  - a) 45.47



**b)** 836.05 m + 988.66 m





13. Oden purchased three snacks for \$1.99, \$2.35, and \$0.65, including tax. He has \$5.00 to pay the bill. Without finding the total, decide whether or not Oden has enough money. Show how you know.

Parcel A is heavier than parcel B by 2.5 kg. Parcel C is lighter than parcel B by 4.86 kg. How heavy is parcel A if parcel C is 6.2 kg?

# 2.2 Multiply Decimal Numbers

MathLinks 7, pages 56-63

## Key Ideas Review

**1.** Order from 1 to 3 the steps for multiplying decimals.



#### Name: \_

#### Date:

- **4.** Estimate and then calculate.
  - a) 2.6 <u>× 5</u> Estimate: \_\_\_\_\_
  - b) 41.2  $\times$  0.3 Estimate:
  - c) 5.2  $\times 3.6$  Estimate:
  - d) 83.1  $\times 0.6$  Estimate: \_\_\_\_\_
  - e) \$525 <u>× 0.5</u> Estimate: \_\_\_\_\_
  - f) 61 × 7.2 Estimate: \_\_\_\_\_
- **5.**  $37.50 \times 207 = 7762.50$ . Use what you know about place values to find each of the following products without multiplying.
  - a) 3.750 × 207 = \_\_\_\_\_
  - **b)** 37.50 × 20.7 = \_\_\_\_\_
  - **c)** 0.3750 × 2.07 = \_\_\_\_\_
  - **d)** 37.50 × 0.207 = \_\_\_\_\_
- **6.** How many times larger is 0.1 than 0.001? Explain your reasoning.

- 7. What is the cost of each purchase before tax? Show your calculations.
  - a) 3 boxes of cereal @ \$4.35 each



b) 3 telephones@ \$19.89 each



c) 12 rolls of duct tape@ \$3.66 each



- 8. Jennifer is a waitress in a restaurant. She is paid \$8.35 per hour. Last week she worked three hours on Monday, five hours on Tuesday, four hours on Thursday, and six hours on Friday.
  - a) How many hours did Jennifer work last week?
  - b) How much did she earn last week? Show your work.
- **9.** Without calculating the answer, circle the larger value. Explain your thinking.

| a) 2.1 × 0.8        | or | 2.1 	imes 0.9 |
|---------------------|----|---------------|
| b) $0.9	imes 0.9$   | or | 1             |
| <b>c)</b> 5.6 + 5.6 | or | 1.9 	imes 5.6 |

Date: \_\_\_\_\_

# 2.3

# **Divide Decimal Numbers**

MathLinks 7, pages 64-71

# **Key Ideas Review**

Match the method of estimating the answer to a division problem with the examples. Write the method from column B that matches each example in column A.

| Α  | В   |
|--|---|
| <ul> <li>1. Estimate 6.6 ÷ 2.3</li> <li>6 ÷ 2 = 3</li> </ul>   | a) Number line<br>estimation                    |
| 2. $(-)$ $($ | b) Estimate, then<br>use a calculator           |
| $6 \div 2 = 3$ underestimate<br>$8 \div 2 = 4$ overestimate  | c) Divide as whole<br>numbers,<br>then estimate |
| <b>3.</b> [C] 25.73 $[\div$ ] 3.1 $[=$ ] 8.3<br>24 $\div$ 3 = 8<br>27 $\div$ 3 = 9<br>The estimates suggest an   | to place the<br>decimal                         |
| answer between 8 and 9. The answer 8.3 is reasonable.  | d) Relative size<br>estimation                  |
| 4. Divide $20.4 \div 3$ .<br>$ \begin{array}{c} \frac{68}{3} \\ 204 \\ \underline{180} \\ 24 \end{array} $ $ \begin{array}{c} 21 \div 3 = 7 \\ \text{The answer is around 7. The decimal point goes between the 6 and 8. \end{array} $   | e) Front-end<br>estimation                      |
| $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  | f) Model the equation                           |

Practise and Apply

 Without calculating the answer, place the decimal point in the correct position. Show the estimate that helped you place the decimal point.

\_\_\_\_\_÷ \_\_\_\_\_ = \_\_\_\_\_

\_\_\_\_\_÷ \_\_\_\_ = \_\_\_\_

**a)**  $82.4 \div 20 = 412$ 

**b)**  $3.12 \div 0.6 = 52$ 

c)  $2.132 \div 0.4 = 533$ 

\_\_\_\_\_÷\_\_\_\_= \_\_\_\_

\_\_\_\_\_÷ \_\_\_\_ = \_\_\_

\_\_\_\_\_÷ \_\_\_\_ = \_\_\_\_

**d)**  $27 \div 0.45 = 600$ 

**e)** 4.026 ÷ 0.6 = 671

$$\frac{1}{33.12 \div 6.9 = 48} = -----$$

- **6.** Estimate each answer and show your thinking. Then, use a calculator to determine each answer.
  - a) 5.24  $\div$  0.5 = \_\_\_\_\_
  - **b)** 68.22 ÷ 0.6 = \_\_\_\_\_ Estimate:

Estimate:

- c)  $2.142 \div 0.07 =$
- Estimate: \_\_\_\_\_\_ d) 111.6 ÷ 4 = \_\_\_\_\_
  - Estimate: \_\_\_\_\_
- **7.** What is the cost of each purchase before tax? Show your calculations.
  - a) 3 oatmeal bars for \$7.50

|   | TTAL DAD  |  |
|---|-----------|--|
|   | TMEAL BAR |  |
| 0 | Arm       |  |
|   |           |  |

 8. George has \$10.50 to spend on energy bars. How many can he buy if they cost \$0.70 each, including tax?

9. Carmen earns \$8.30 per hour.
She wants to buy a jacket that costs \$124.50.
How many hours will she have



to work to have enough money to buy the jacket? Estimate, then use a calculator to determine the answer.

b) 5 cans of tuna for \$5.30



c) 6 lemons for \$2.99



- 10. Without calculating the answer, circle the larger value. Explain your thinking.
  a) 7.8 ÷ 0.98 or 7.8 ÷ 1
  - **b)** 16 ÷ 0.5 or 25
  - c) 1500 or  $2 \div 0.001$
  - **d)** 9.3 ÷ 1.02 or 9.3
  - e) 536  $\div$  0.72 or 536  $\div$  0.68

# 2.4 Order of Operations and Decimal Numbers

MathLinks 7, pages 72–77

**Key Ideas Review** 

1. a) Find the words in the puzzle.

| ADD      | MULTIPLY |
|----------|----------|
| SUBTRACT | DIVIDE   |
| BRACKETS |          |

| Q | U | S | А | А | D | L | В | Μ |
|---|---|---|---|---|---|---|---|---|
| A | Μ | U | L | Т | Ι | Р | L | Y |
| В | R | А | С | Κ | ۷ | R | Т | L |
| 0 | R | D | Ε | R | Ι | 0 | С | Р |
| D | R | А | 0 | R | D | Ε | А | А |
| A | Е | Р | С | S | Е | D | R | L |
| S | R | А | С | Κ | Е | Т | Т | Ε |
| A | D | D | Е | Κ | Е | R | В | М |
| C | 0 | R | D | А | D | Т | U | R |
| Т | С | А | R | Т | В | U | S | Μ |

**b)** Order the words from #1a) in the correct order of operations.

| STEP 1: |     |          |
|---------|-----|----------|
| STEP 2: | and | in order |
| STEP 3: | and | in order |

**2.** Put brackets in the following expressions to get the largest values possible.

| a) $5 + 6 \div 3 \times 2$ | b) |
|----------------------------|----|
| c) $9 + 3 \div 6 + 5$      | d) |

Practise and Apply

- **3.** Place the two operations shown in square brackets to make each statement true.
  - a) 8 \_\_ 3.1 \_\_ 4 = 20.4 [+, ×]
  - **b)** 16 \_\_\_ 8 + 9.3 \_\_\_ 7.8 = 3.5 [-, ÷]
  - c) (6.1 \_ 4.3) \_ 4 = 7.2 [-,  $\times$ ]
  - **d)** (15.4 \_\_ 3.6) \_\_ 4 = 4.75 [+, ÷]

- **b)**  $5 + 4 \times 4 \div 2$ **d)**  $18 + 3 - 3 \times 5$
- **4.** Place brackets to make each statement true.
  - a) 7 + 5  $\times$  3.2 = 23
  - **b)** 10.6 + 4.4 8.1 3.1 = 10
  - c)  $16 \div 4 + 5 1 = 8$
  - d)  $15.5 6.5 \times 3 = 27$
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5. Mr. Lang needed to pick up a few groceries. He bought two boxes of cereal at \$6.95 each, three loaves of bread at \$1.69 each, and four litres of apple juice at \$0.89 a litre. He had two grocery coupons: one for \$1.50 and the other \$1.75.



 a) Estimate the total cost of the groceries. There is no tax on food. Is your estimate high or

\$1.50

- low? Explain how you know.
- b) Estimate the total cost of the groceries if Mr. Lang uses both coupons.
- c) Calculate the total cost of groceries if Mr. Lang uses both coupons.
- Luke plays the saxophone.
   One week he practised for the following amounts of time.



\$1.75

| Day       | Hours Practised |
|-----------|-----------------|
| Monday    | 1.2 h           |
| Wednesday | 2.1 h           |
| Friday    | 1.6 h           |
| Sunday    | 2.8 h           |

- a) Estimate the average number of hours Luke practised per day.
- **b)** Calculate the total number of hours Luke practised per week.
- c) If Luke practised the same number of hours for five weeks in a row, how many hours in total would he have practised?
- What are the missing numbers? Show how you know.
  - a) \_\_\_\_\_ + 3.4 × 26 = 94.6
  - **b)** 7 + 6.4  $\div$  \_\_\_\_\_ = 7.8
  - c)  $8 + 5.3 \times \_\_\_ = 21.25$
  - d) 21 2.5 × \_\_\_\_ = 7.5
- 8. Calculate.
  - a)  $5 \times 6.3 =$  \_\_\_\_\_
  - **b)**  $5 \times (6 + 0.3) =$
  - c)  $5 \times 6 + 5 \times 0.3 =$  \_\_\_\_\_
  - d) What do you notice about your answers in parts a-c)? Explain why this is the case.

# **Link It Together**

 Zach wants to make a pet collar for his dog, Hudson. At the pet store, he finds a collar for \$6.95. He also finds letters for \$1.95 each and decorations for \$2.50 each. The store is having a "no tax" day.





a) How much will it cost to buy a collar with the following design? Show your calculation in two different ways.



- **b)** Zach has \$30.00 from his birthday. If he wants the collar to include Hudson's full name plus some decorations, how many decorations can he buy?
- c) Design a collar for a dog or cat. How much would this collar cost?

# **Vocabulary Link**

Use the clues to identify the key words from Chapter 2. Then, write them in the crossword puzzle blank.

#### Across

- **1.** This example shows \_\_\_\_\_:  $(5.3 + 2.7) \times 3 = 24$ .
- 2. When you \_\_\_\_\_\_, you calculate an approximate answer. The symbol  $\approx$  means "is approximately equal to."

#### Down

**1.** An estimate that is larger than the actual answer is called a(n)

\_\_\_\_\_. For example, 235 + 376 is approximately 676.

- **3.** The following example uses \_\_\_\_\_\_ estimation. 235 + 376  $\approx$  200 + 300  $\approx$  500
- **4.** The following example uses \_\_\_\_\_\_ estimation. 235 + 376  $\approx$  200 + 400  $\approx$  600
- 5. An estimate that is smaller than the actual answer is called a(n)

\_\_\_\_\_. For example, 235 + 376 is approximately 576.

